

Collisionless MHD turbulence in the intracluster medium of galaxies

Reinaldo Santos-Lima (USP, Brazil)



Magnetic Fields in the Universe V
Cargese - Oct 5-9, 2015

Collaborators:

E. M. de Gouveia Dal Pino (USP, Brasil)

H. Yan (KIAA, China; DESY, Germany)

A. Lazarian (UW, USA)

D. Falceta-Gonçalves (USP, Brasil)

G. Kowal (USP, Brasil)

M. S. Nakwacki (UBA, Argentina)

Intracluster Medium is turbulent and magnetized

Major sources of turbulence:

- cosmological mergers of subclusters
- AGNs and galactic winds

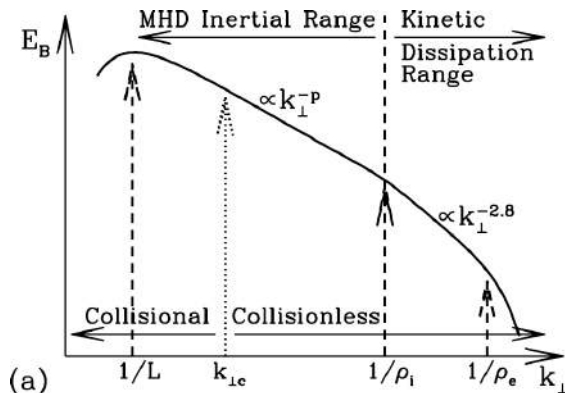
Origin of magnetic fields in the ICM: small-scale dynamo

MHD simulations of subclusters merger show the amplification of seed magnetic fields in the ICM until $\sim \mu\text{G}$ (Kotarba et al. 2011).

(See K. Dolag's talk)

Seed fields: Biermann Battery, deposition by AGNs and galactic winds, primordial origin...

Turbulence cascade in the ICM



(a)

(from Howes 2012)

Scales

$$L_{turb} \sim 500 \text{ kpc}$$

$$\lambda_i \sim 30 \text{ kpc}$$

$$\rho_i \sim 10^5 \text{ km}$$

$$\rho_e \sim 10^3 \text{ km}$$

ICM collisionless scales:

- Large scale motions (turbulence) + conservation of magnetic moment of charged particles \rightarrow anisotropy in the thermal velocities distribution;
- Anisotropy in the thermal velocities distribution \rightarrow instabilities;
- Instabilities important for ions: ion-cyclotron, mirror, firehose;
- Maximum linear growth rate for unstable modes at scales \sim ion Larmor radius;

What is the role of the above collisionless effects in the ICM dynamics?

Collisionless MHD: two-temperature description

- Collisions frequency not high enough to relax the ions velocity distribution to a Maxwellian during dynamical time scales;
- Better approximation: bi-Maxwellian (two temperatures);
- Thermal pressure tensor: $P_{ij} = p_{\perp} \delta_{ij} + (p_{\parallel} - p_{\perp}) \mathbf{b}_i \mathbf{b}_j$;
- Mirror and firehose instabilities present in the **anisotropic** (two-temperature) MHD fluid description:

$$\frac{\partial}{\partial t} \begin{bmatrix} \rho \\ \rho \mathbf{u} \\ \mathbf{B} \end{bmatrix} + \nabla \cdot \begin{bmatrix} \rho \mathbf{u} \\ \rho \mathbf{u} \mathbf{u} + \Pi_P + \Pi_B \\ \mathbf{B} \mathbf{u} - \mathbf{u} \mathbf{B} \end{bmatrix} = \begin{bmatrix} 0 \\ \mathbf{f} \\ 0 \end{bmatrix}$$

$$\Pi_P = p_{\perp} \mathbf{I} + (p_{\parallel} - p_{\perp}) \mathbf{b} \mathbf{b}, \quad \Pi_B = (B^2/8\pi) \mathbf{I} - \mathbf{B} \mathbf{B}/4\pi$$

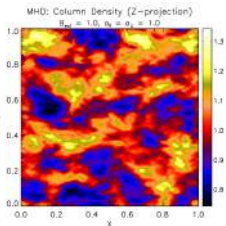
(G. Kowal's talk)

Collisionless MHD: double isothermal closure

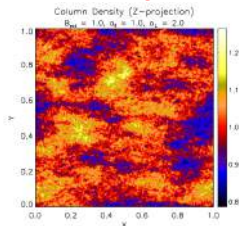
$$p_{\perp} = c_{\perp}^2 \rho \quad p_{\parallel} = c_{\parallel}^2 \rho$$

Kowal, Falceta-Gonçalves & Lazarian (2011)

MHD

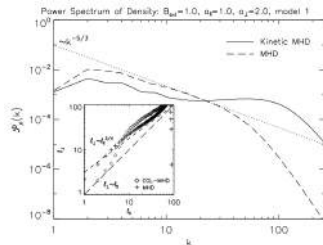


Mirror



$(c_{\perp}/c_{\parallel} = 2, \text{trans-S, sub-A})$

Velocity power spectrum



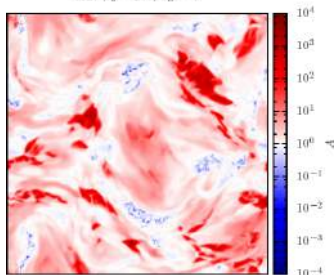
Conservation of particles magnetic momentum and entropy

$$\frac{d}{dt} \left(\frac{p_{\perp}}{\rho B} \right) = 0 \quad \frac{d}{dt} \left(\frac{p_{\parallel} B^2}{\rho^3} \right) = 0$$

(Chew, Goldberger & Low 1956)

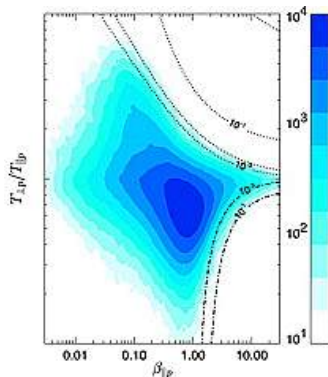
$$A = T_{\perp} / T_{\parallel}$$

A2: $\beta_0 = 200, \nu_S = 0$



(Santos-Lima et al. 2014)

- Anisotropy in pressure/temperature observed to saturate in solar wind, plasma experiments and PIC simulations (Marsh 2006, Keiter 1999, Riquelme et al. 2012)



(from Hellinger et al. 2006)

- Electromagnetic fluctuations from the instabilities scatter particles, reducing anisotropy.

Bounded Anisotropy model (Denton et al. 1994)

$$\frac{dT_{\perp}}{dt} = \left(\frac{dT_{\perp}}{dt} \right)_{CGL} + \nu_S (T_{\parallel} - T_{\perp})$$

$$\frac{dT_{\parallel}}{dt} = \left(\frac{dT_{\parallel}}{dt} \right)_{CGL} + 2\nu_S (T_{\perp} - T_{\parallel})$$

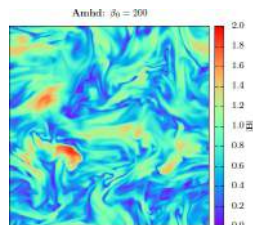
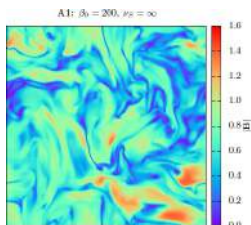
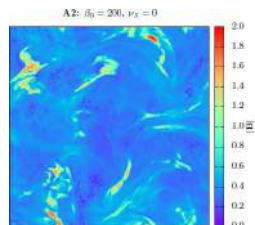
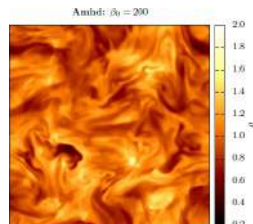
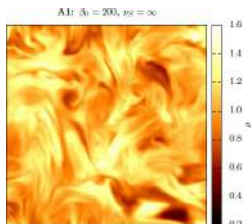
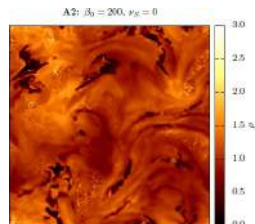
- $\nu_S (B, T_{\perp}, T_{\parallel})$ has to be determined by theory or kinetic calculations for each instability;

Santos-Lima, de Gouveia Dal Pino, Kowal, Falceta-Gonçalves, Lazarian, Nakwacki (2014)

Turbulence and small-scale dynamo in the intra-cluster medium:

- Modified Godunov code (Kowal et al. 2011);
- Forced turbulence (trans-sonic, super-Alfvénic) in a periodic box;
- $\beta_0 = 200$;
- Parameter study of the ions scattering: from $\nu_S = 0$ (CGL-MHD) to $\nu_S = \infty$

Collisionless MHD turbulence: numerical simulations



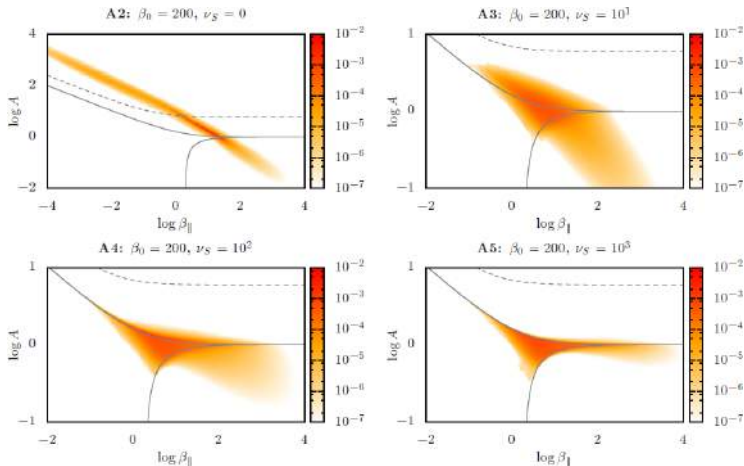
collisionless MHD
no relaxation (CGL)

collisionless MHD
instant. relaxation

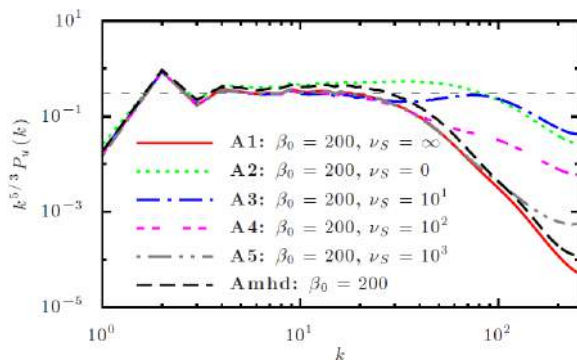
MHD

Collisionless MHD turbulence: numerical simulations

$$\text{Log } p_{\parallel} / (B^2 / 8\pi) \quad \times \quad \text{Log } T_{\perp} / T_{\parallel}$$



Velocity power spectrum ($\times k^{5/3}$)



MHD

no relaxation (CGL)

$$\nu_S = 0$$

finite relaxation

$$\nu_S \sim 10^1 t_{turb}^{-1}$$

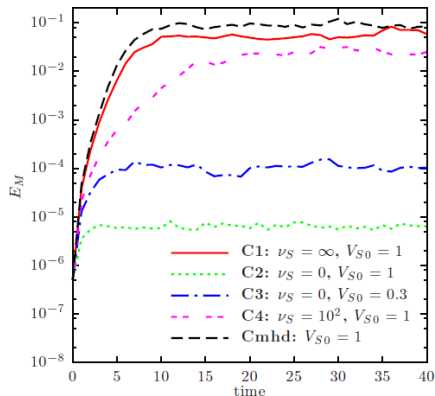
finite relaxation

$$\nu_S \sim 10^2 t_{turb}^{-1}$$

instant. relaxation

$$\nu_S = \infty$$

Time evolution of the magnetic energy



MHD

no relaxation (CGL)

$$\nu_S = 0$$

no relaxation (CGL)

$\nu_S = 0$, supersonic

finite relaxation

$$\nu_S \sim 10^2 t_{turb}^{-1}$$

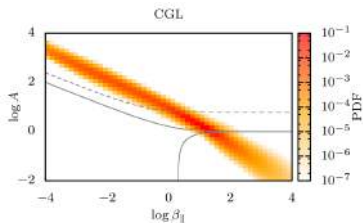
instant. relaxation

$$\nu_S = \infty$$

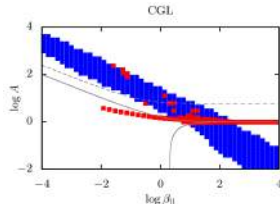
Ions scattering rate: quasi-linear calculations

- Scattering of ions by the parallel ion-cyclotron + parallel firehose modes

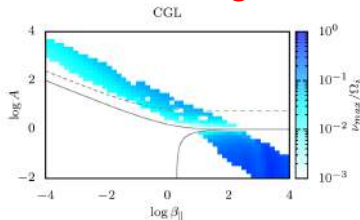
initial parameters



after 2000 Larmor periods



max. scattering rates



ICM:

$$\Omega_i \sim 10^{-2} \text{ rad/sec}$$

$$\tau_{turb}^{-1} \sim 10^{-16} \text{ sec}$$

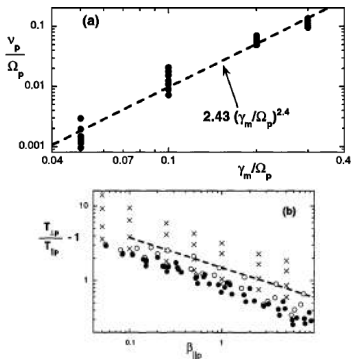
$$(B \sim 1 \mu\text{G},$$

$$L_{turb} \sim 500 \text{ kpc},$$

$$U_{turb} \sim 10^3 \text{ km/s})$$

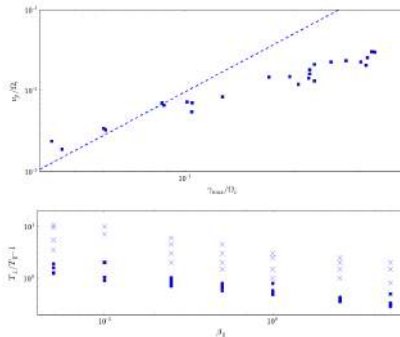
Ions scattering rate: quasi-linear vs. 2D PIC

2D PIC



(from Gary et al. 2000)

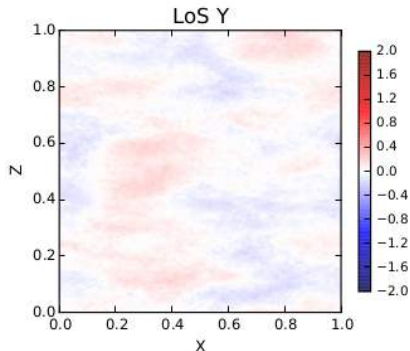
Quasi-linear (ion-cyclotron modes only)



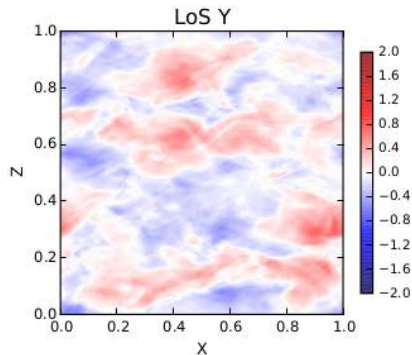
Synthetic RM maps (1): constant temperatures models

- Faraday screen: periodic data cubes with **double isothermal MHD** turbulence models (Kowal et al. 2011);
- Effects of large (fluid) scales instabilities.

Mirror ($c_{\perp}/c_{\parallel} = 2$, trans-S, sub-A)



MHD

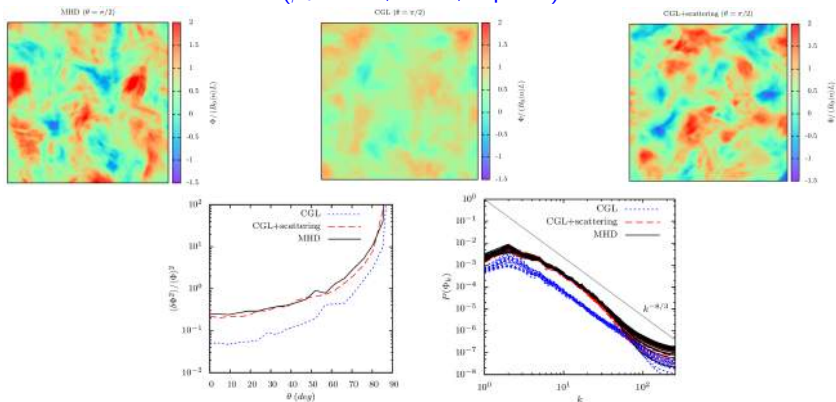


(Nakwacki, Kowal, Santos-Lima,
de Gouveia Dal Pino, Falceta-Gonçalves, 2015)

Synthetic RM maps (2): CGL + scattering models

- Faraday screen: periodic data cubes with CGL-MHD (+ scattering) turbulence models (Santos-Lima et al. 2014);
- Effects of the particles scattering.

($\beta_0 = 200$, sub-S, super-A)



Summary

- Collisionless MHD models for the ICM: two temperatures \rightarrow coupling between thermal and magnetic stresses \rightarrow firehose and mirror instabilities;
- Development of temperature anisotropies due to local changes of (\mathbf{B}, ρ) + scattering of ions by the plasma instabilities at the kinetic scales;
- Limit of fast scattering of ions:
 - temperature anisotropy is pushed to marginal stability levels;
 - the turbulence statistics and magnetic field amplification \approx one temperature MHD;
 - statistics of RM maps \approx one temperature MHD;
- Limit of no scattering of ions:
 - most of plasma inside unstable regime, predominance of $T_{\perp} > T_{\parallel}$;
 - turbulence statistics \rightarrow deviation from one temperature MHD;
 - **no** magnetic field amplification via small-scale dynamo;
 - statistics of the RM maps \rightarrow smaller dispersion, changes in power spectrum;
- Quasi-linear plasma calculations point to **fast** scattering of ions.