

Statistical properties of polarized dust emission : lessons from a toy model of the turbulent and magnetized interstellar medium

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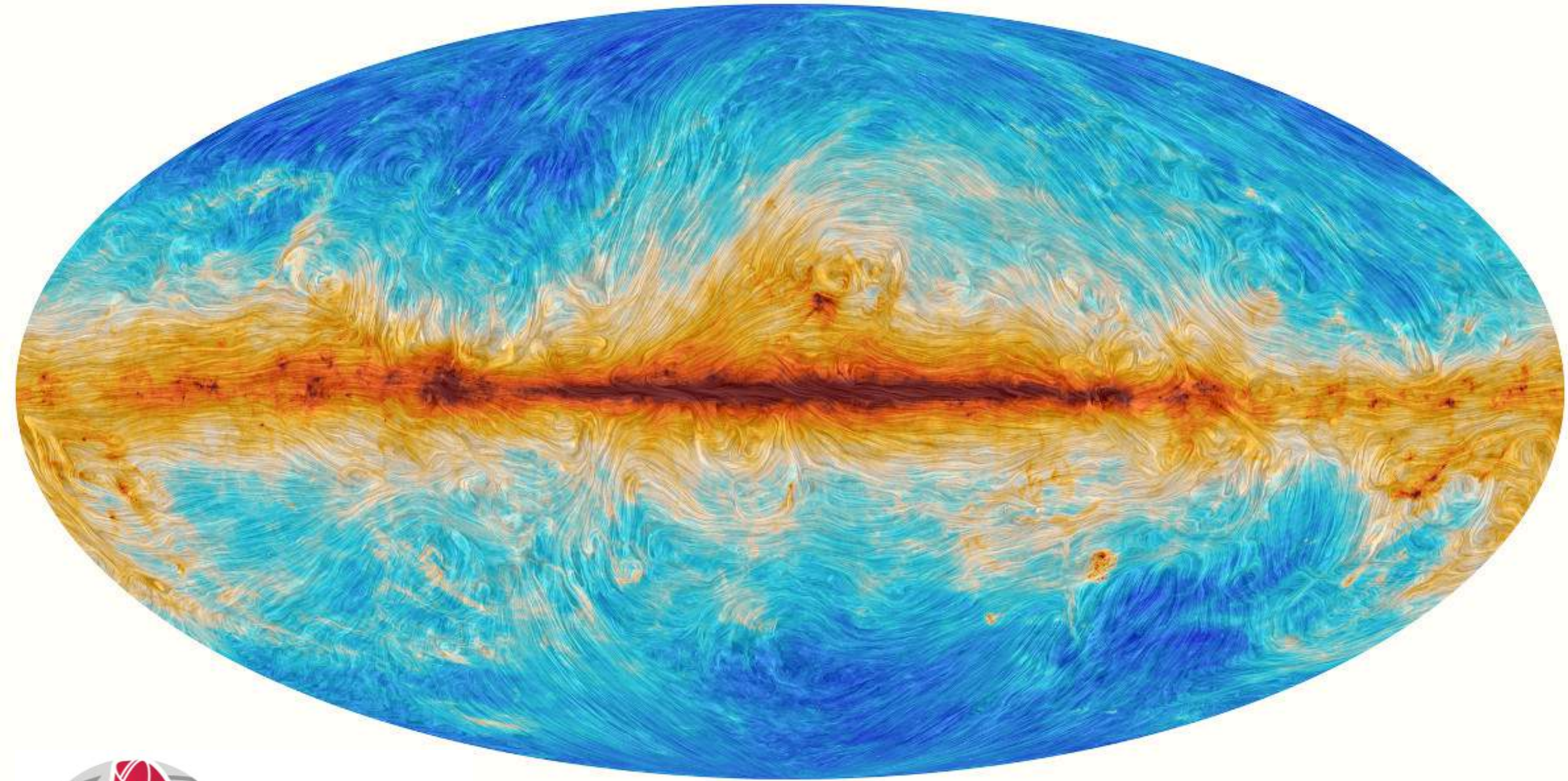
Thanks to Jérémy Neveu



Laboratoire d'Étude du Rayonnement et de la Matière en Astrophysique

Magnetic Fields in the Universe V, Cargèse, 5-9 October 2015

The Planck view of the Galactic magnetic field



planck

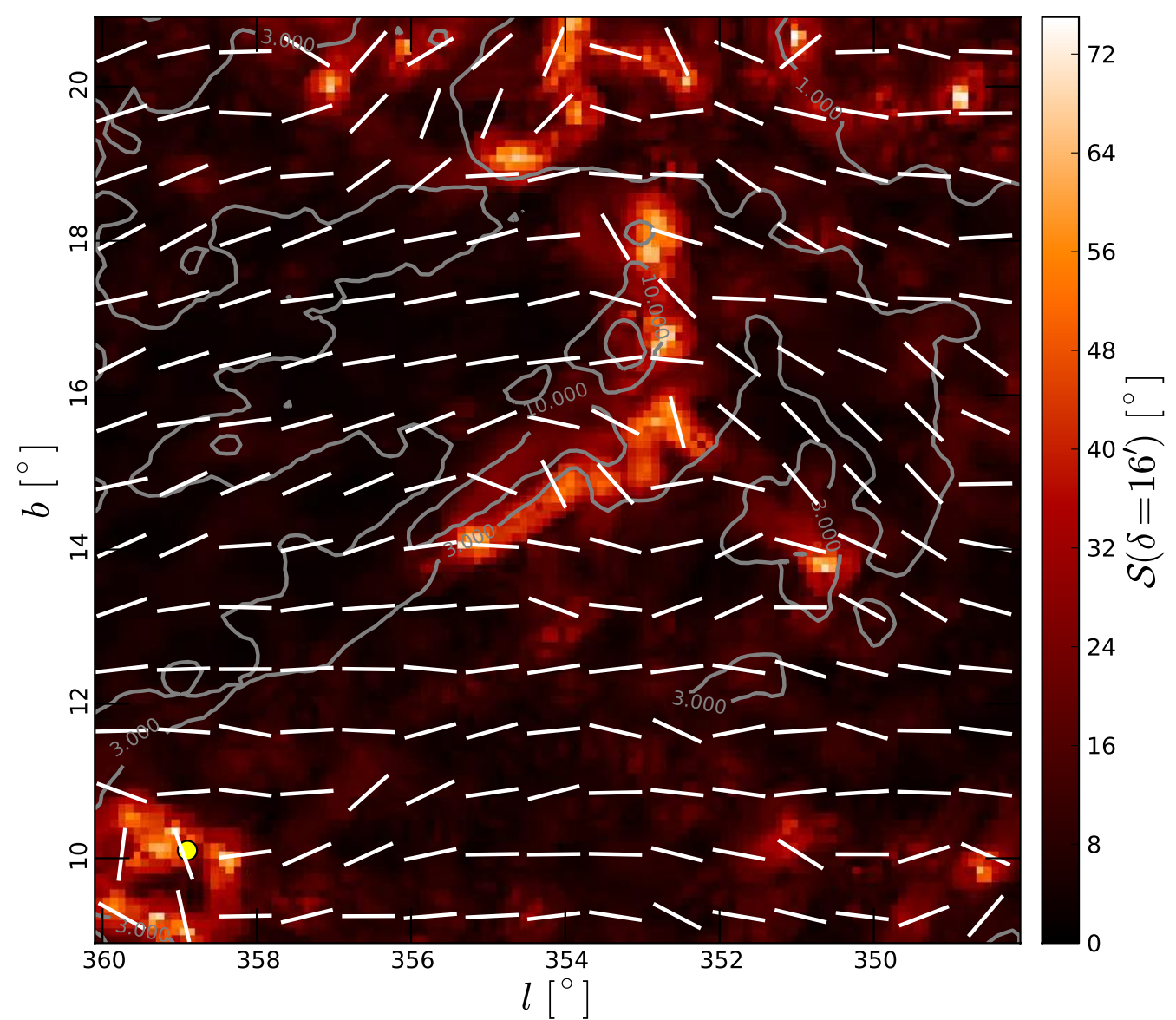
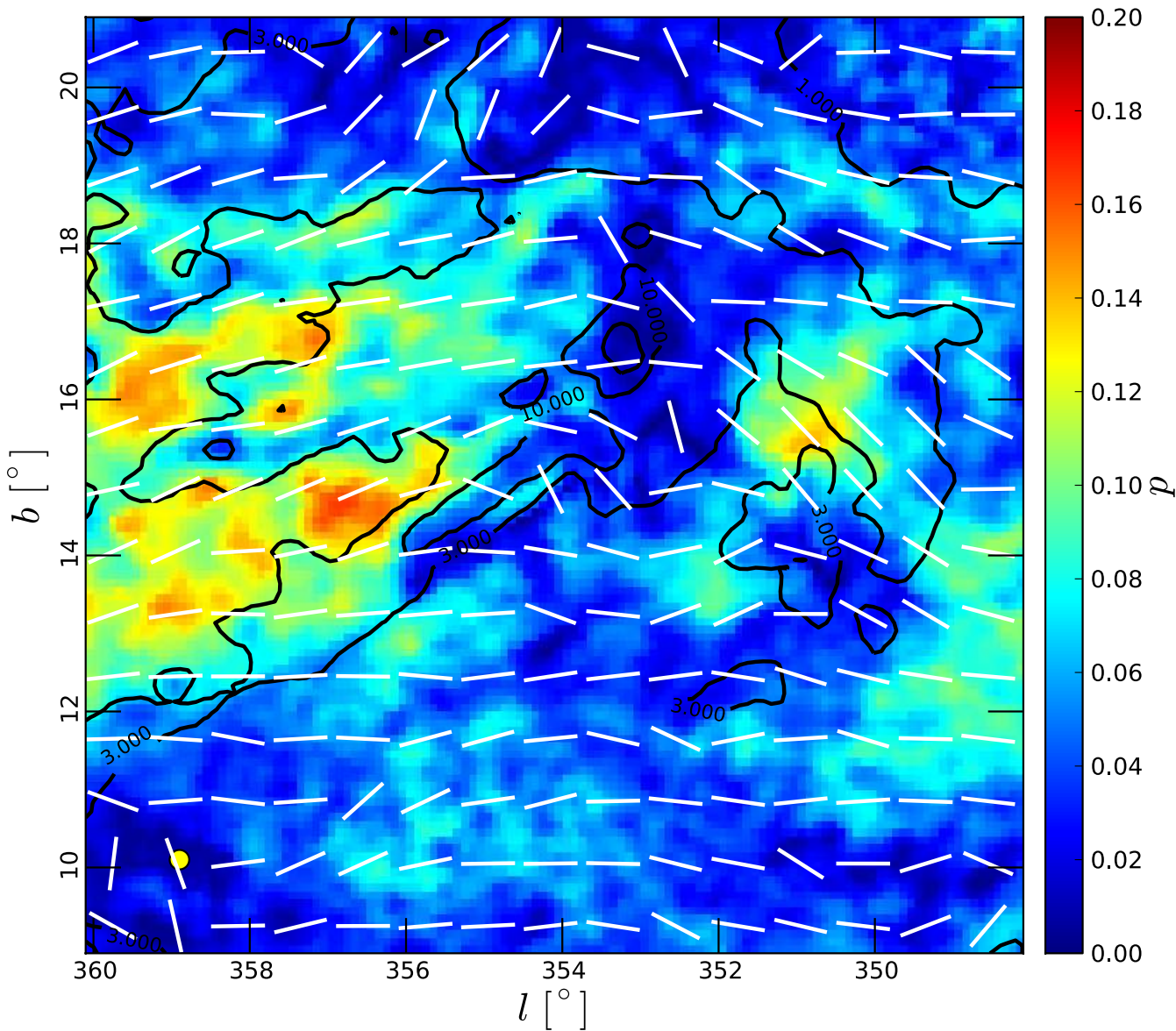
Polarized emission towards Ophiuchus

Polarization fraction

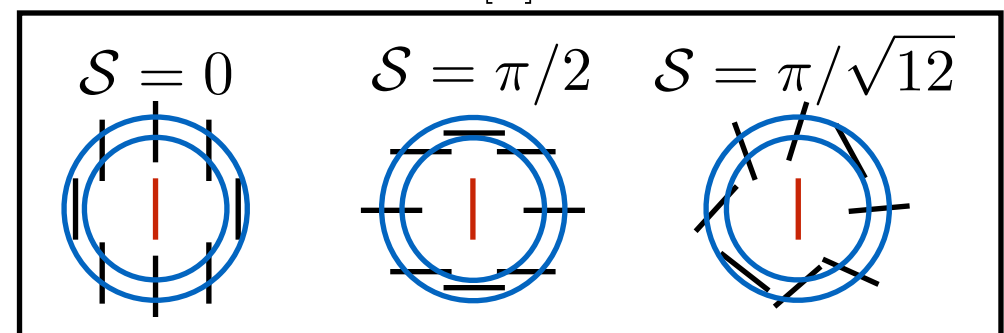
$$p = \frac{\sqrt{Q^2 + U^2}}{I}$$

Polarization angle dispersion function

$$S(\mathbf{r}, \delta) = \sqrt{\frac{1}{N} \sum_{i=1}^N [\psi(\mathbf{r} + \delta_i) - \psi(\mathbf{r})]^2}$$



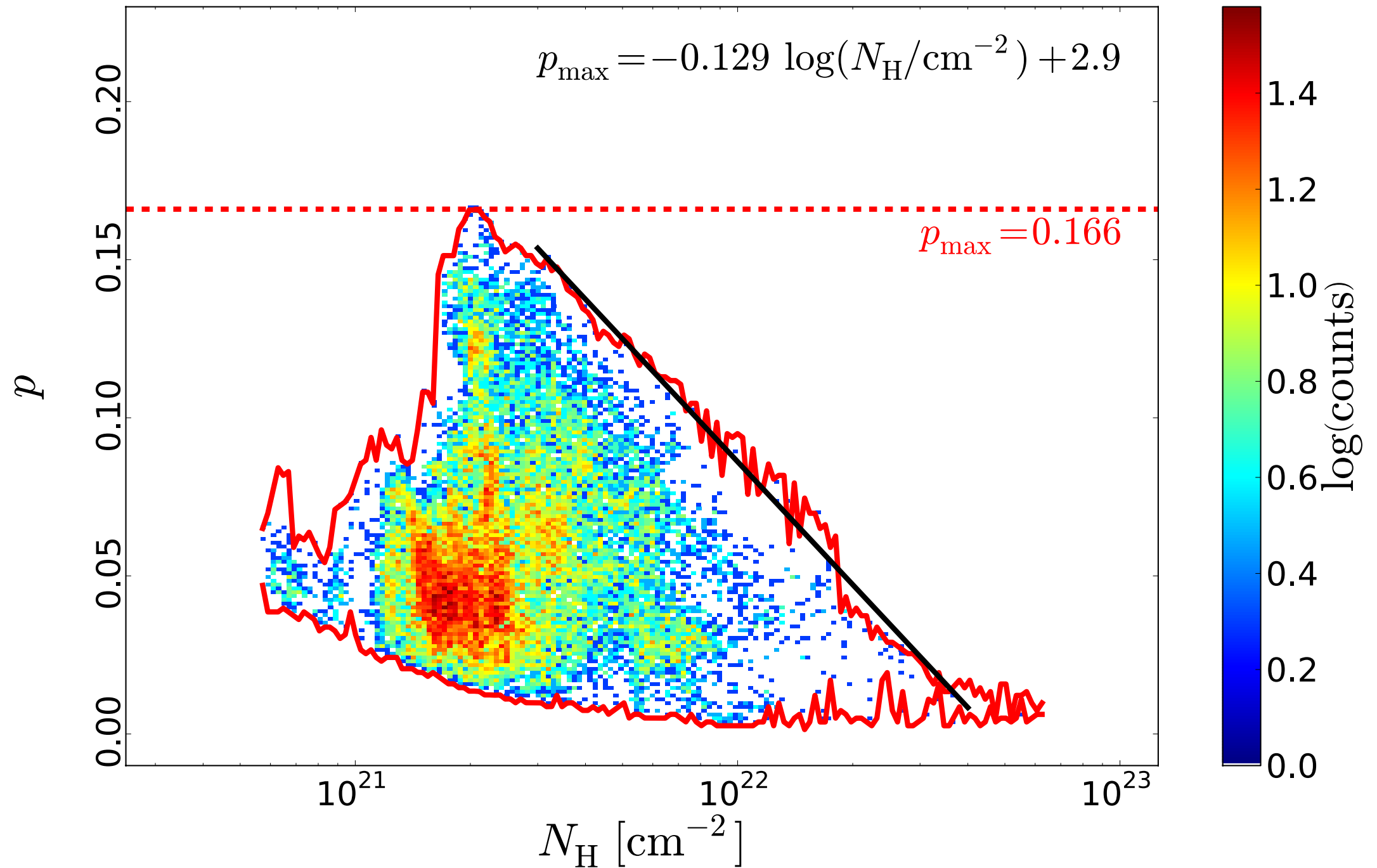
15' resolution
16' lag δ



Polarization fraction vs. column density

$$p/\sigma_p > 3$$

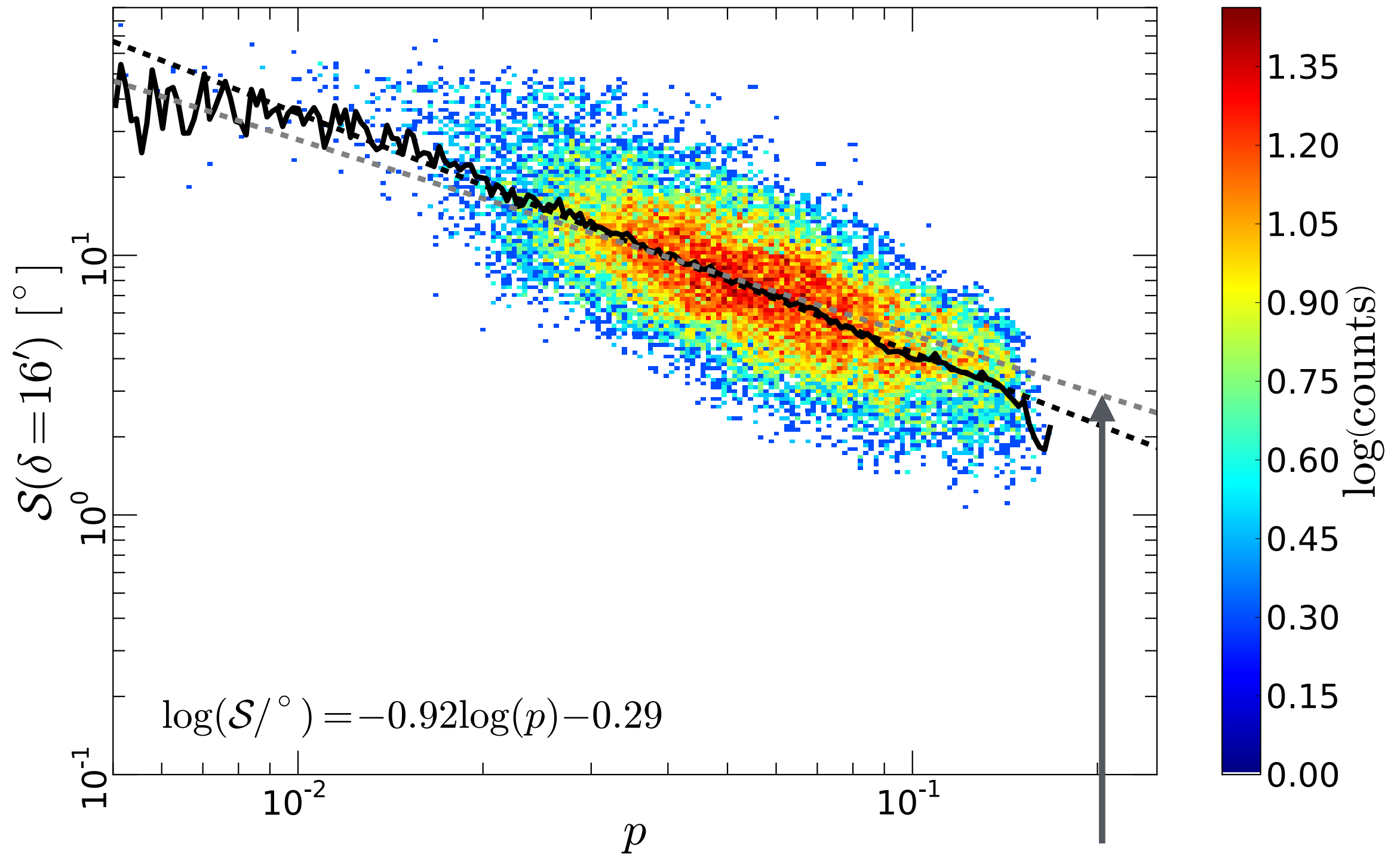
Ophiuchus



Anti-correlation robust with respect to polarization S/N

Angular dispersion vs. polarization fraction

Ophiuchus



« All-sky » fit

Building simulated polarized emission maps

- Ideal MHD with self-gravity
- An 18 pc subset of a 50 pc simulation cube
- Converging flows of magnetized warm gas
- Mean magnetic field along the flows
- Rotation of the cube, placed at 100 pc
- Simulated Stokes maps at 353 GHz smoothed at 15'

$$I = \int S_\nu e^{-\tau_\nu} \left[1 - p_0 \left(\cos^2 \gamma - \frac{2}{3} \right) \right] d\tau_\nu$$

$$Q = \int p_0 S_\nu e^{-\tau_\nu} \cos(2\phi) \cos^2 \gamma d\tau_\nu$$

$$U = \int p_0 S_\nu e^{-\tau_\nu} \sin(2\phi) \cos^2 \gamma d\tau_\nu$$

« Intrinsic dust polarization parameter »

$$p_0 = 0.2$$

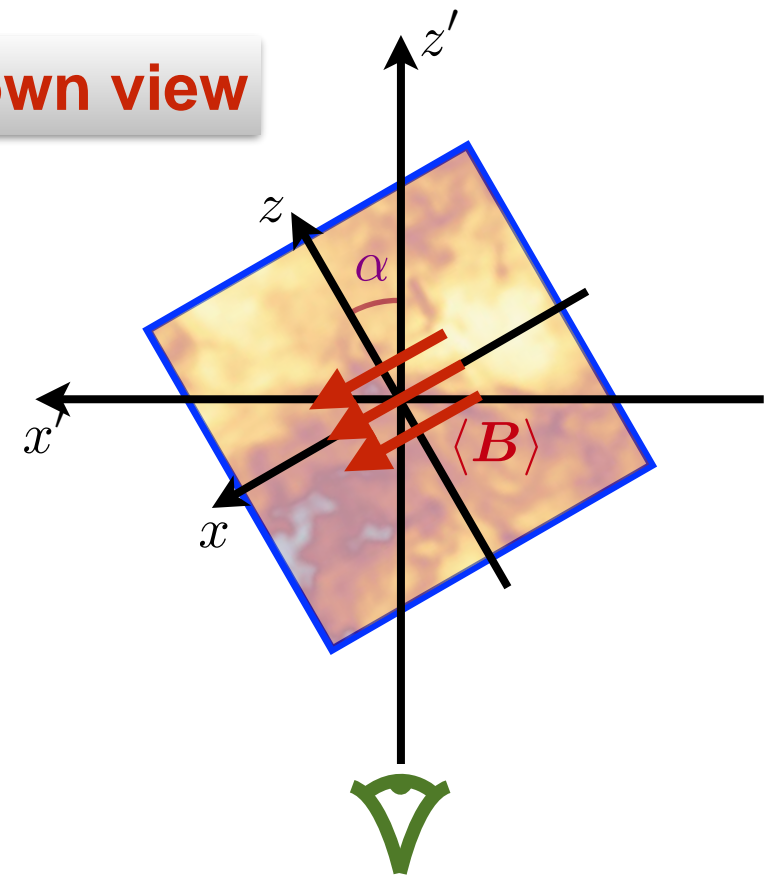
Opacity at 353 GHz (Planck Collaboration XXXI, 2014)

$$\tau_{353}/N_H = 1.2 \times 10^{-26} \text{ cm}^2$$

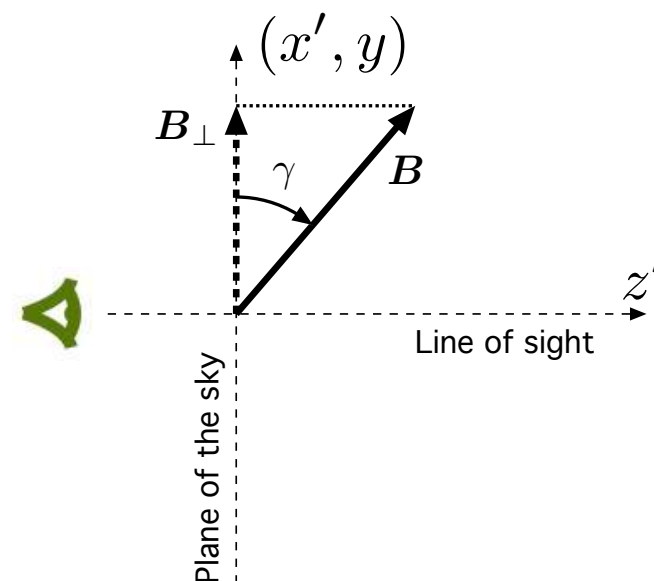
Dust temperature

$$T_d = 18 \text{ K}$$

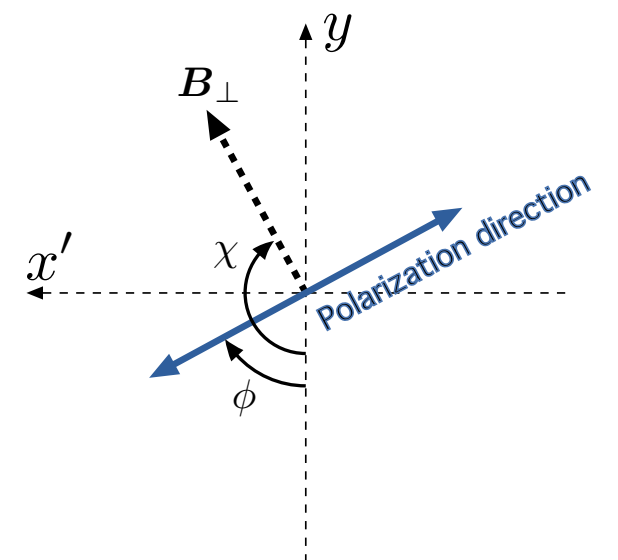
Top-down view



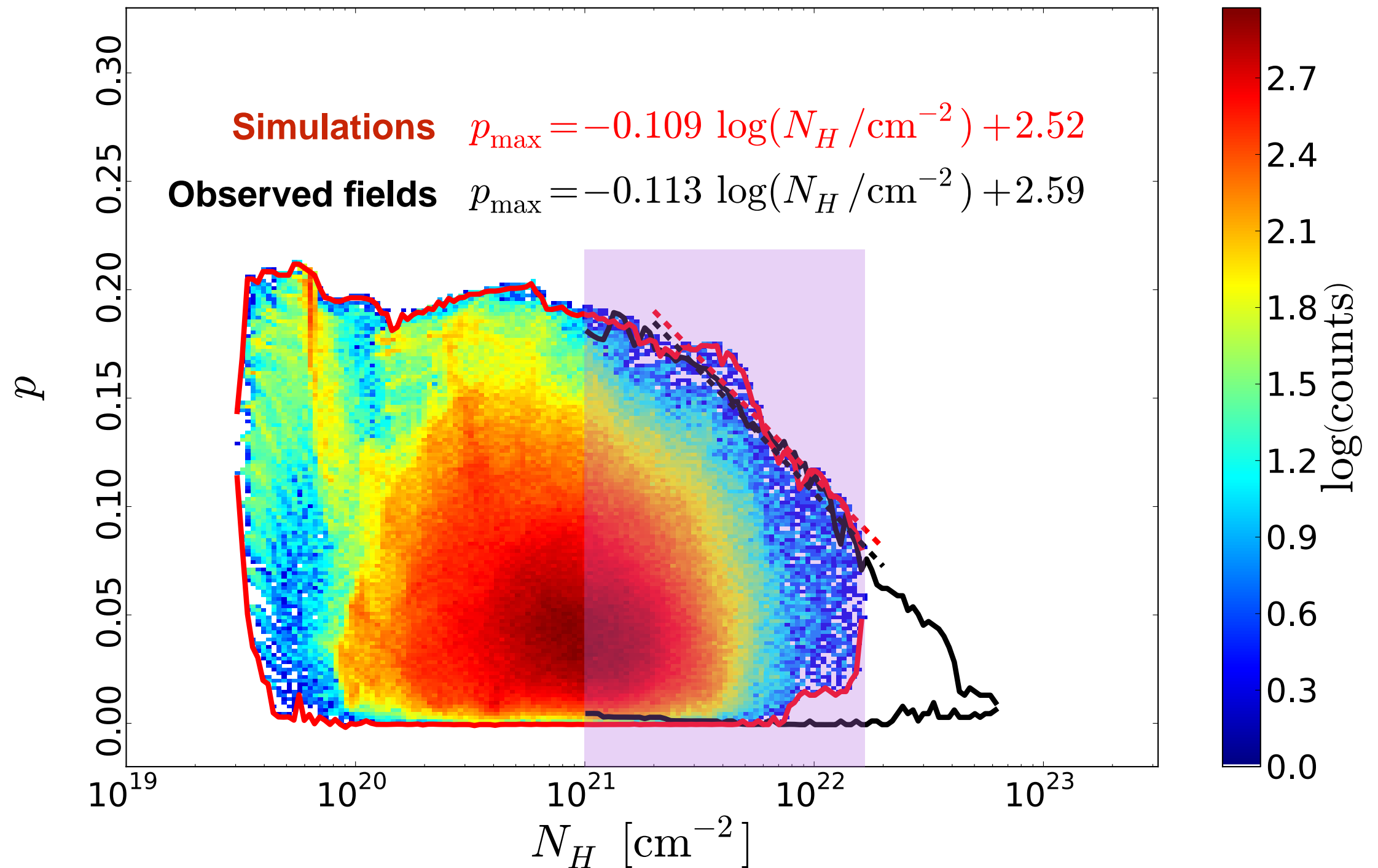
Side view



Line-of-sight view

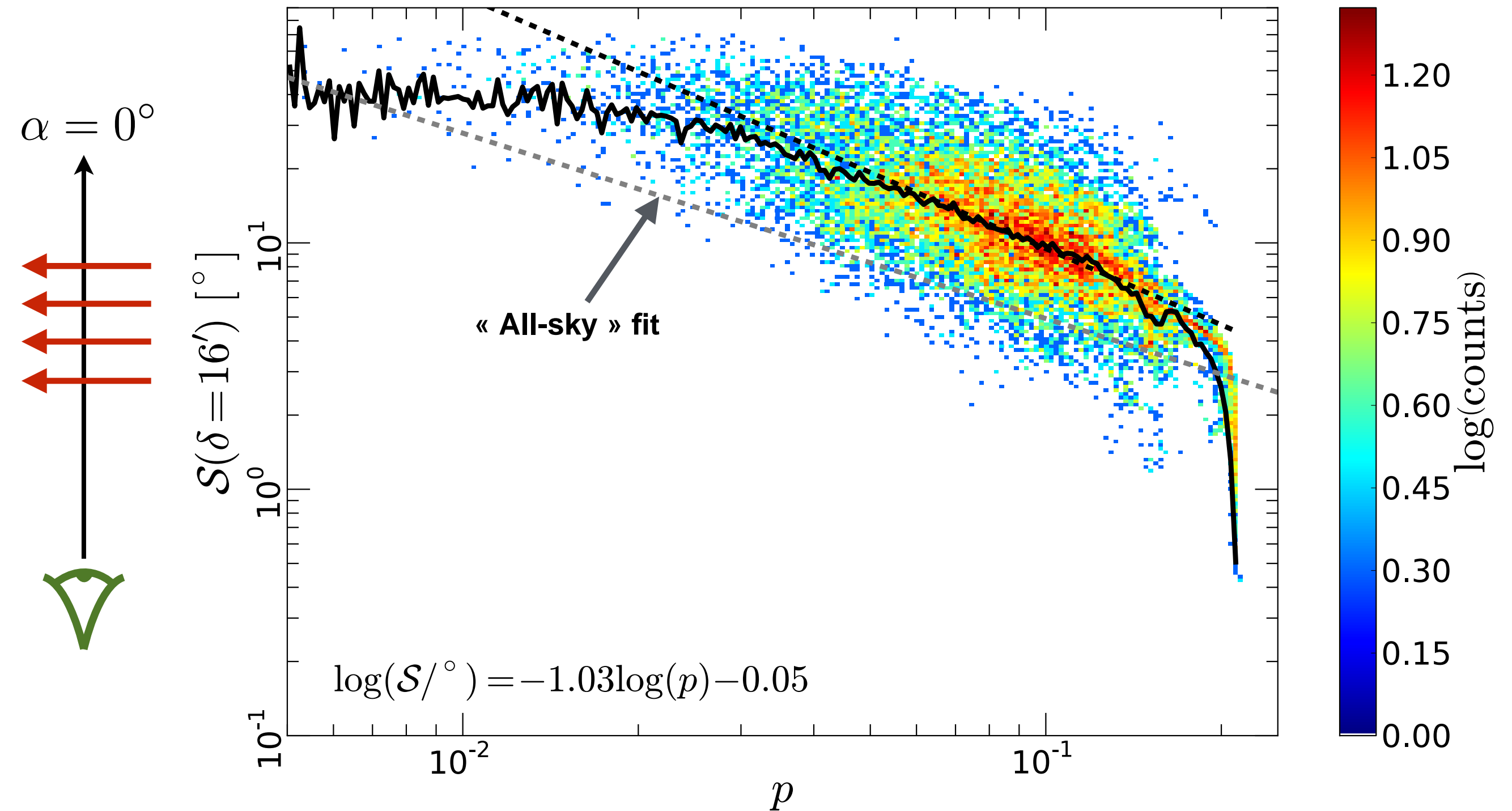


Simulations vs. Observations



Simulations reproduce very well the decrease of p_{\max} with N_H in the range 10^{21} to $2 \times 10^{22} \text{ cm}^{-2}$

Simulations vs. Observations



Global trend is reproduced, but simulations tend to have too high an angular dispersion

From reality to observables and back again ?

We wish to constrain the statistical properties of the interstellar B field

Physical fields

$n, T, \vec{B}, \vec{v}, \dots$

Observables

$I, Q, U, p, \psi, \mathcal{S}, \dots$

- ▶ **Density spectral index** β_n
- ▶ **B spectral index** β_B
- ▶ **Density fluctuation level** $\sigma_n / \langle n \rangle$
- ▶ **B fluctuation level** $\sigma_B / \langle B \rangle$
- ▶ **Line-of-sight depth** d

...

PDFs

Power spectra

Correlations

...



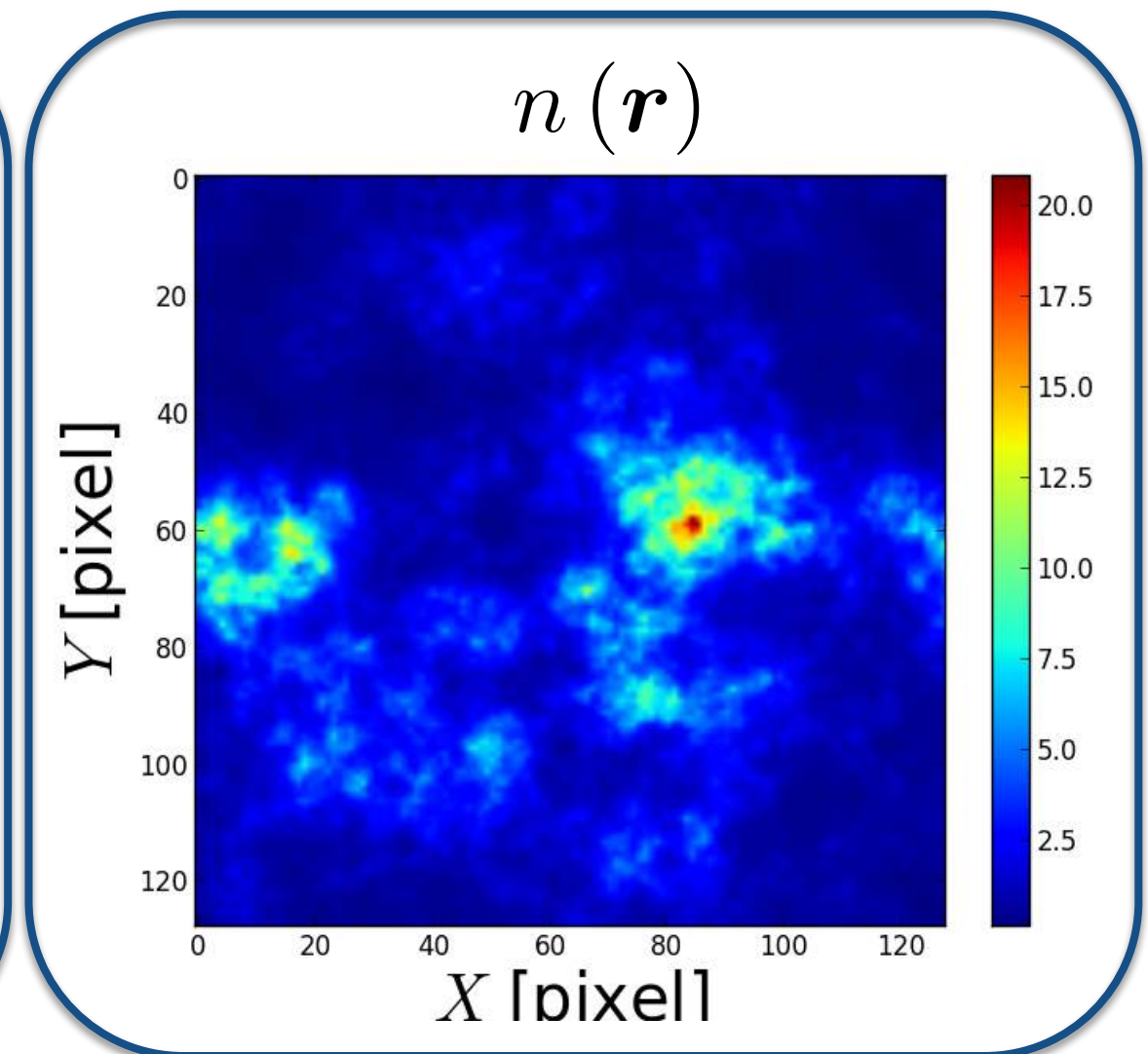
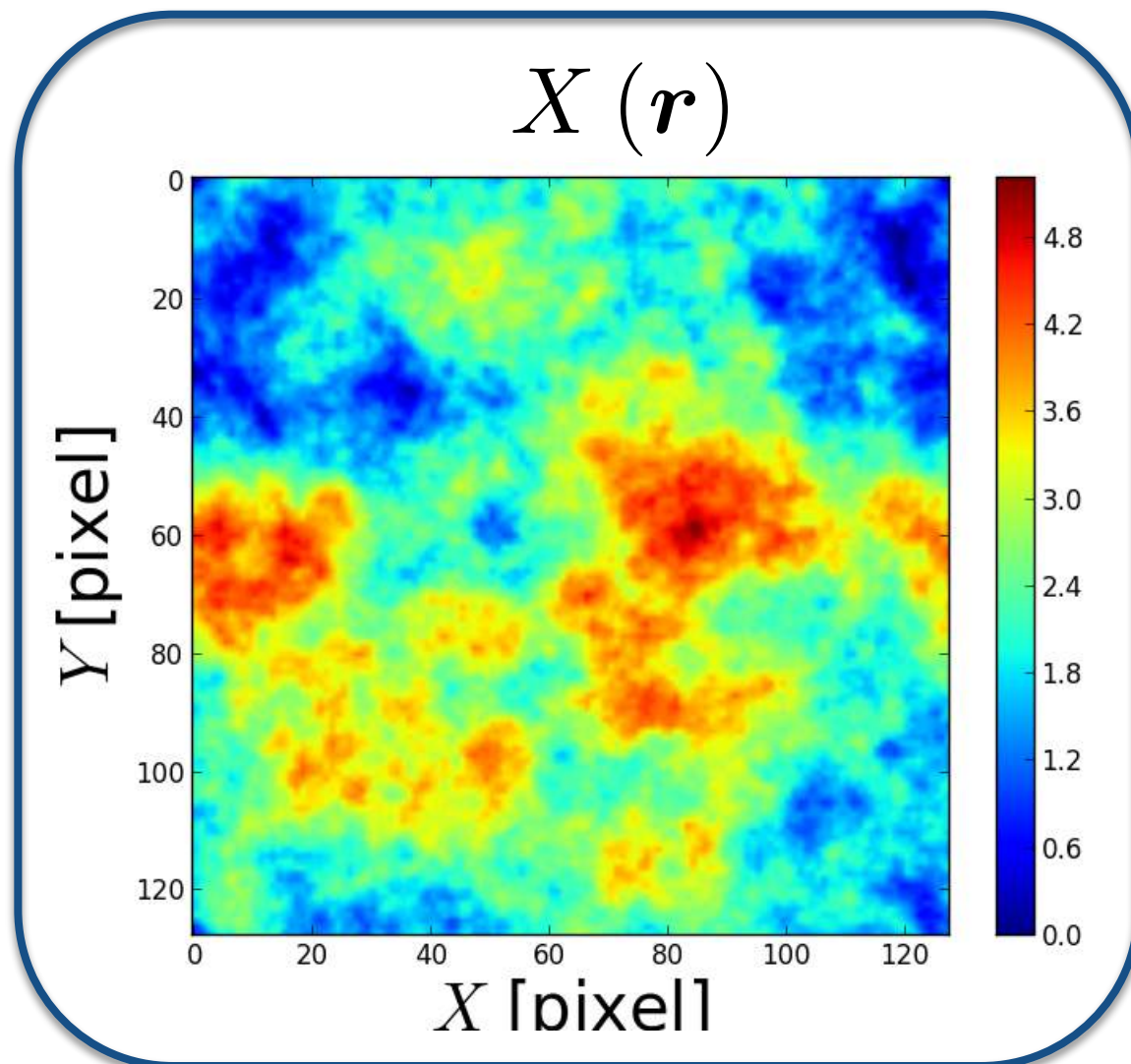
Building a toy dust density field

log-density built as a fractional Brownian motion (fBm)

inverse FT

$$\tilde{X}(\mathbf{k}) = A_0 |\mathbf{k}|^{-\beta} \exp[i\phi(\mathbf{k})]$$
$$n(\mathbf{r}) = n_0 \exp\left[\frac{X(\mathbf{r})}{X_0}\right]$$

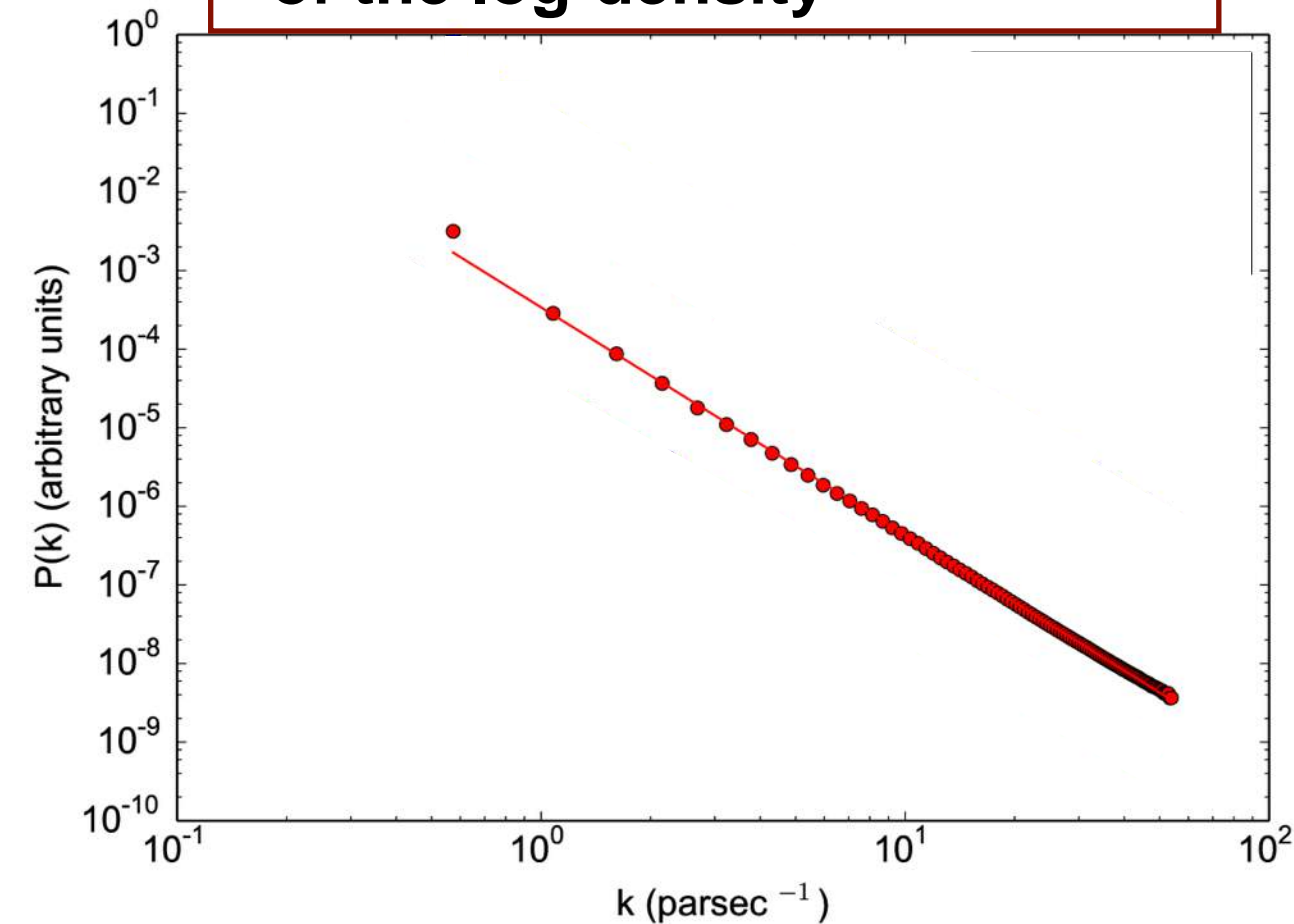
- Power-law amplitudes
- Random phases



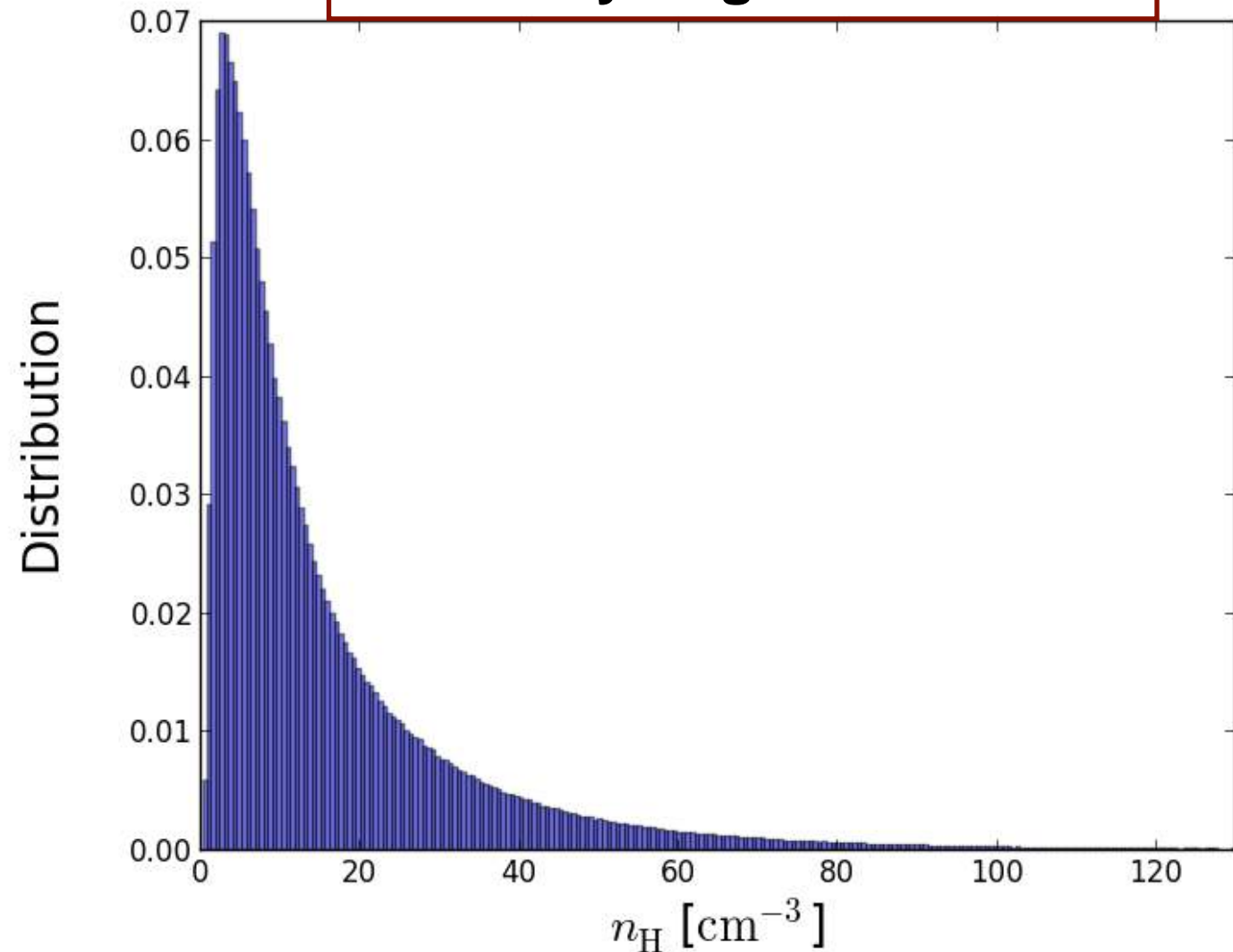
Properties of the toy dust density field

$$n(\mathbf{r}) = n_0 \exp \left[\frac{X(\mathbf{r})}{X_0} \right]$$

- Power-law power spectrum
- Spectral index close to that of the log-density



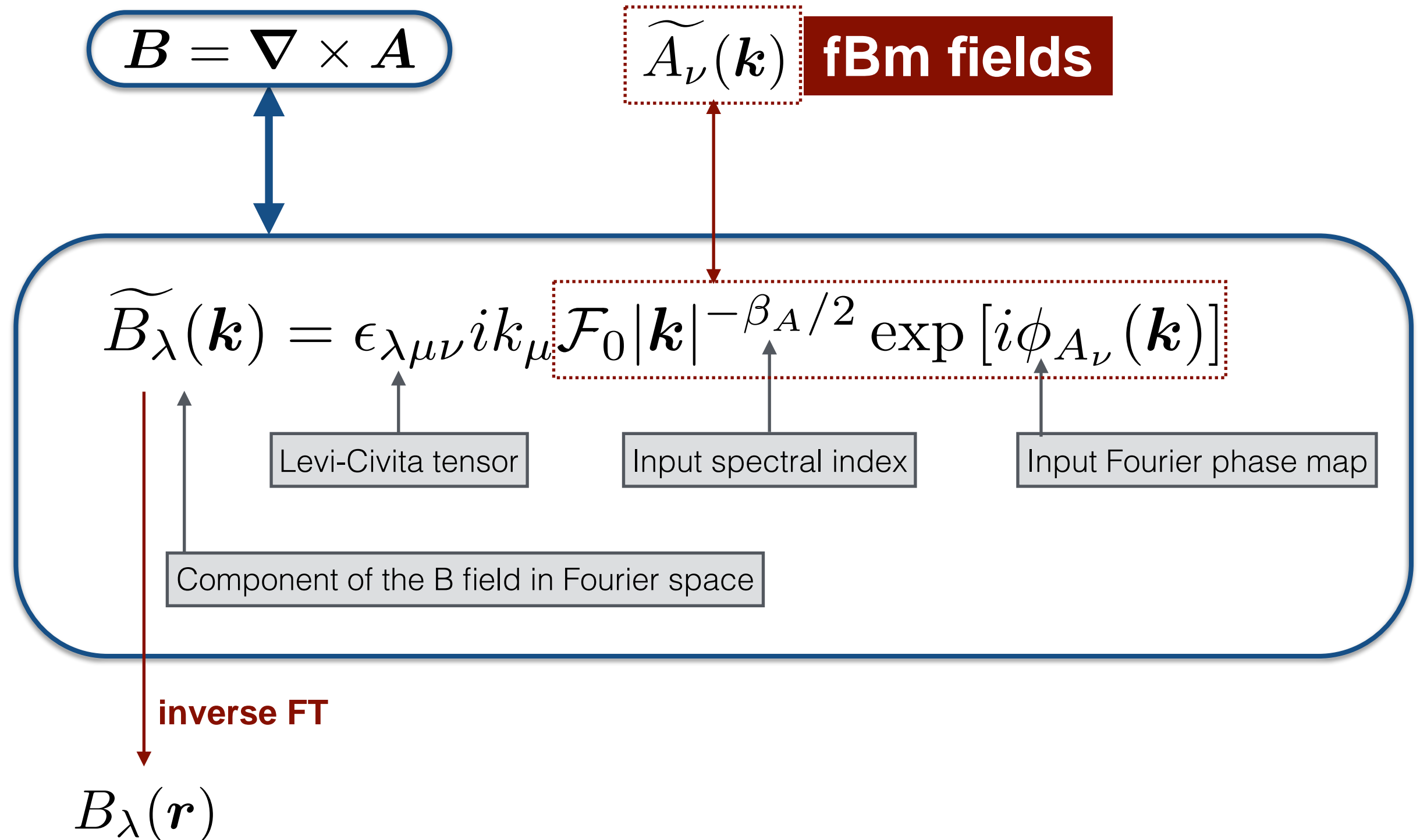
- Close to log-normal PDF
- Possibly large fluctuations



NB : for fBm fields $\frac{\sigma_X}{\langle X \rangle} < 0.3$

Building a toy magnetic field

Magnetic field built from fBm vector potential components

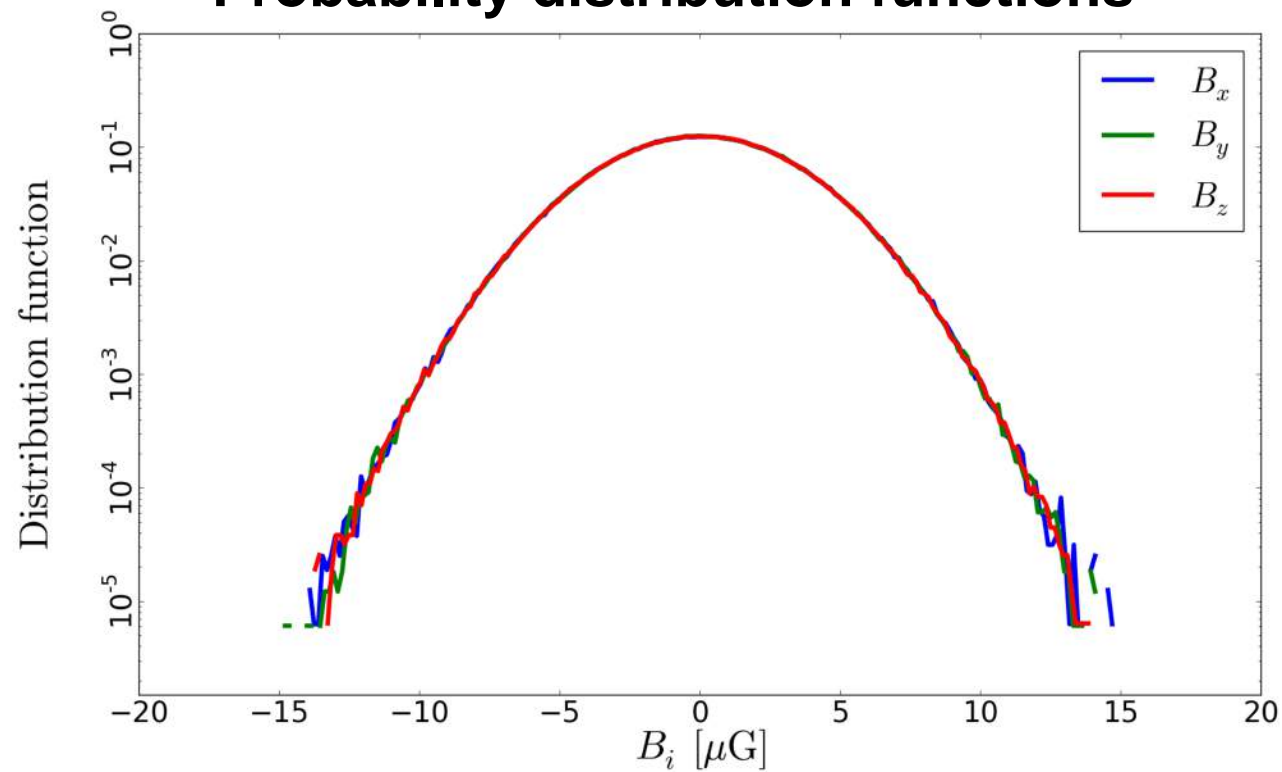


Properties of the toy magnetic field

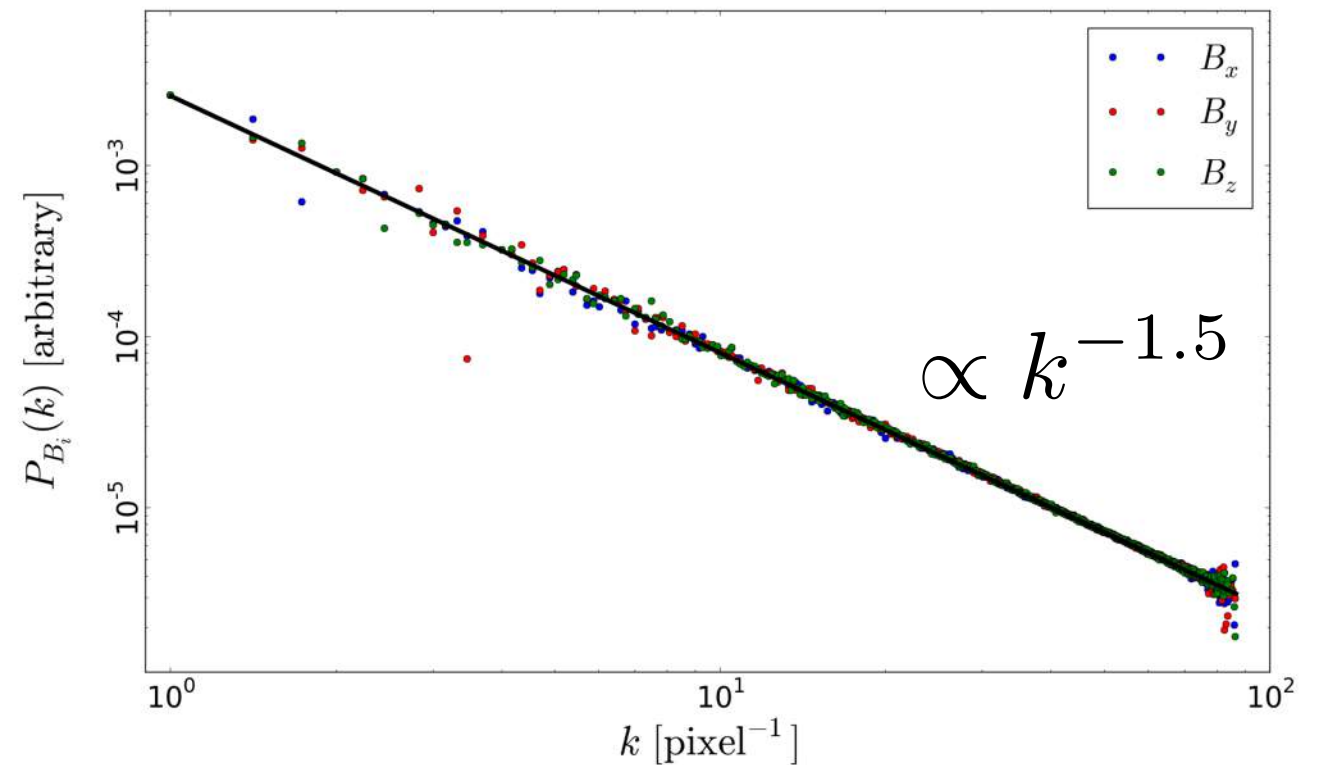
- Divergence-free
- Power-law power spectrum
- Gaussian PDF with zero mean
- Possibility to add a large-scale uniform field

$$\beta_B = \beta_A - 2$$

Probability distribution functions



Power spectra



Physical parameters and observables

Physical parameters of the input cubes

- Spectral indices
- Fluctuation ratios
- Depth

$$\beta_n, \beta_B, \frac{\sigma_n}{\langle n_d \rangle}, \frac{\sigma_B}{\langle B \rangle}, d$$



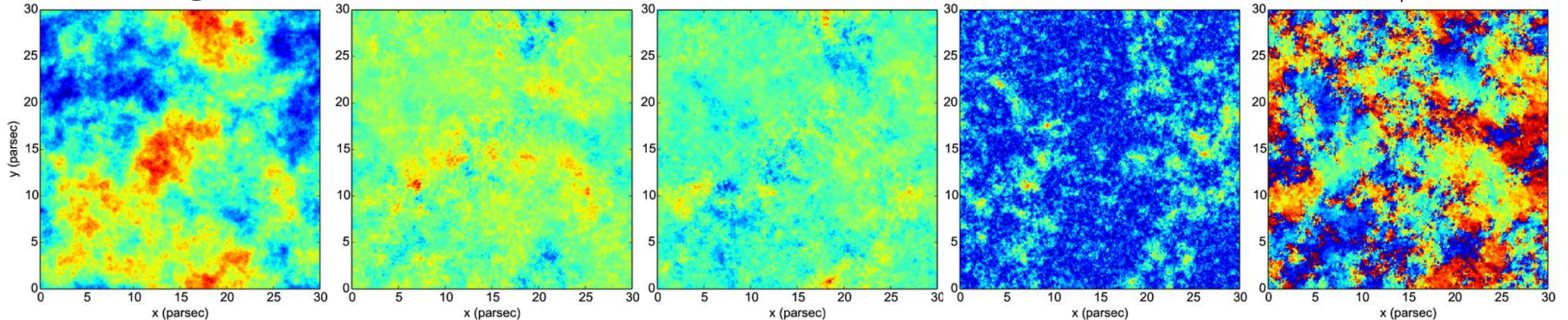
$\log I$

Q

U

p

ψ



Observables derived from simulated Stokes maps

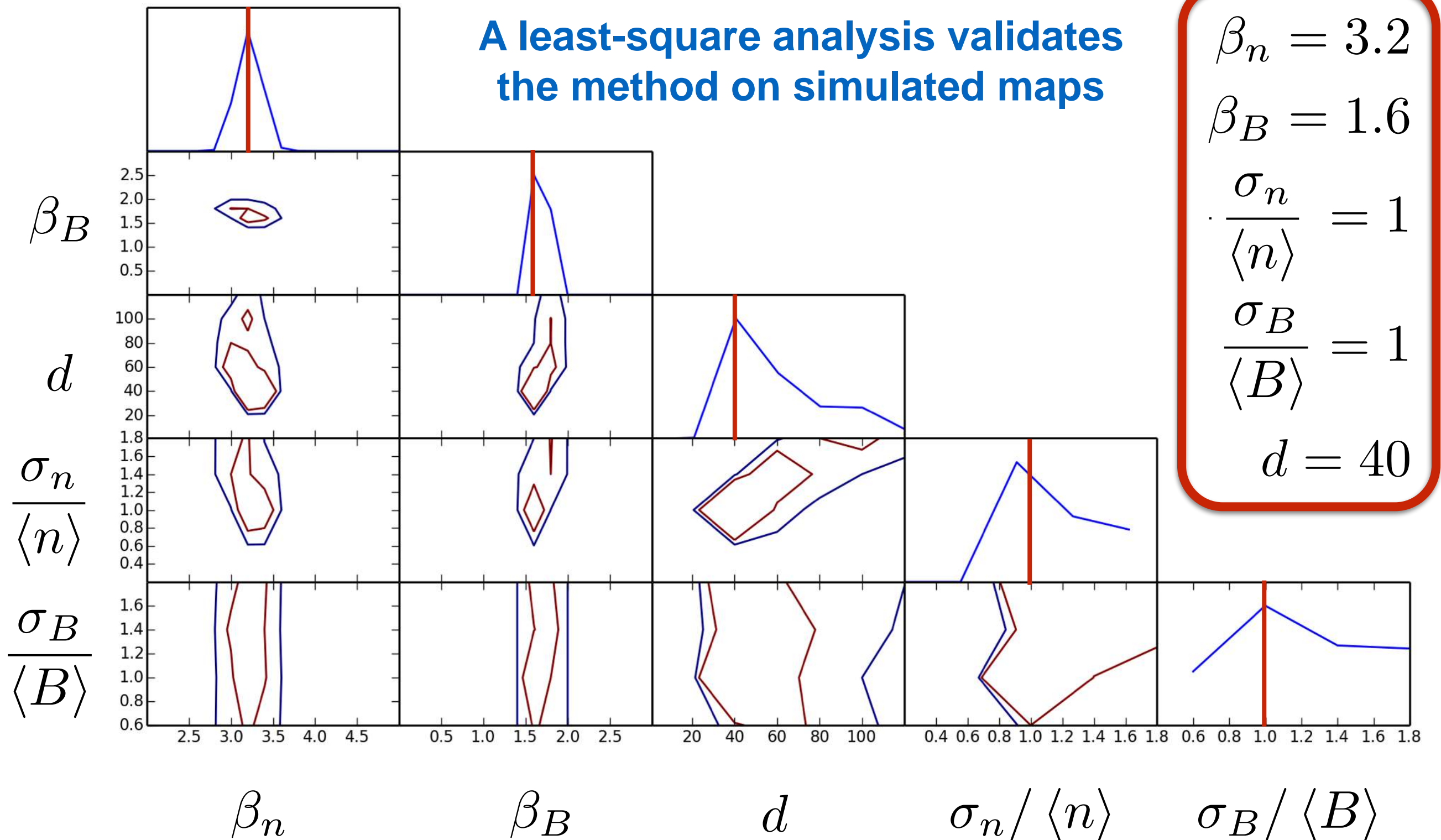
- Spectral indices of I, Q, U, P
- Fluctuation ratios of I, P
- Position of PDF maximum of $\mathcal{S}, p, |\nabla P|/P$
- Correlation \mathcal{S} vs. p
- Correlation \mathcal{S} vs. $|\nabla P|/P$



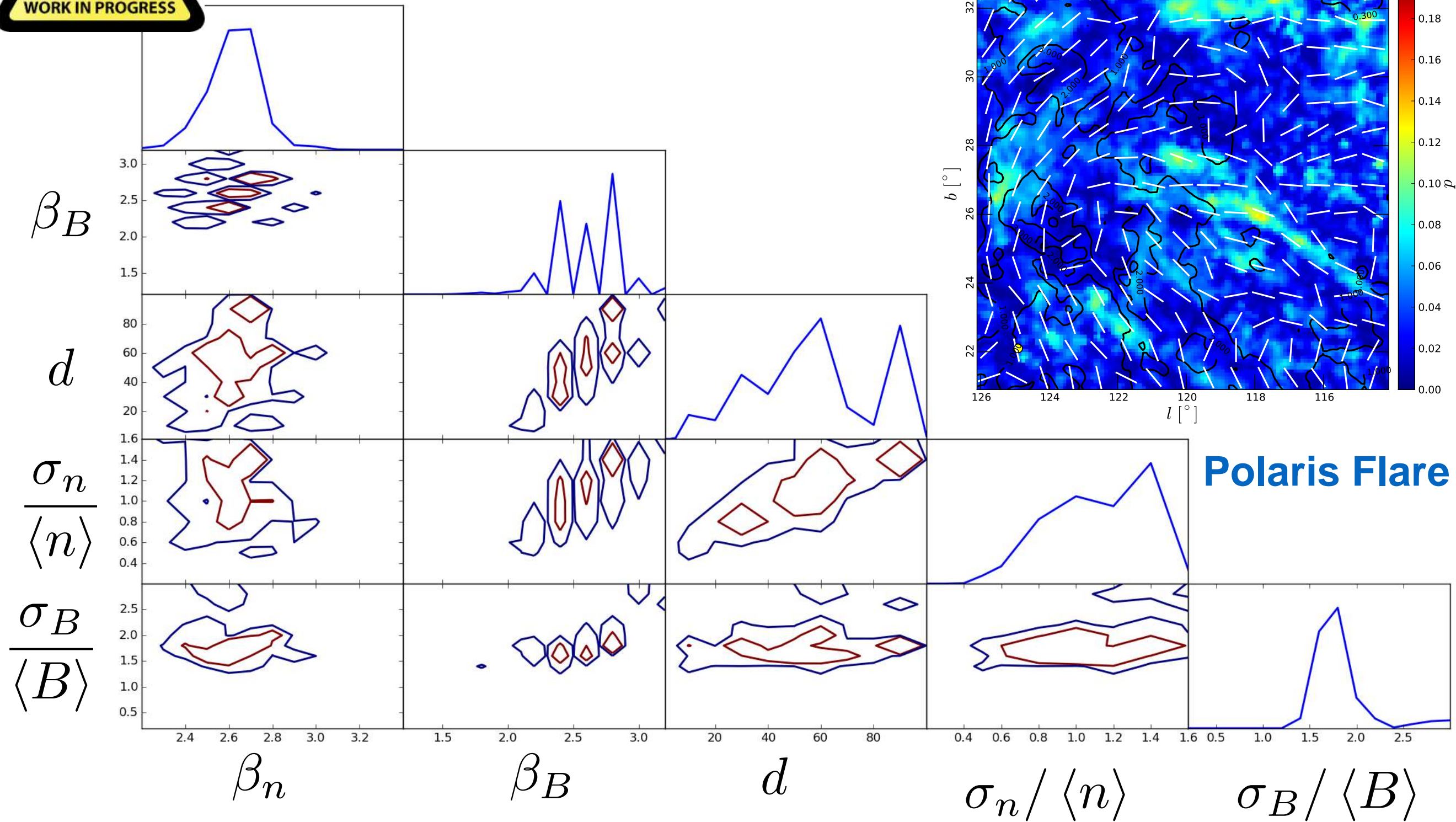


Validating the method

A least-square analysis validates the method on simulated maps



Application to Planck data



- B spectral index near 2.6, consistent with approaches of Bracco and Vansyngel
- Power spectrum tends to steepen with increasing depth

Conclusions

Comparison of Planck polarization maps with MHD simulations

- **Decrease of p_{\max} with N_H well reproduced by simulations**
- **Anticorrelation between polarization fraction and angle dispersion underlines the role of the magnetic field**

Likelihood analysis to constrain statistical properties of ISM B

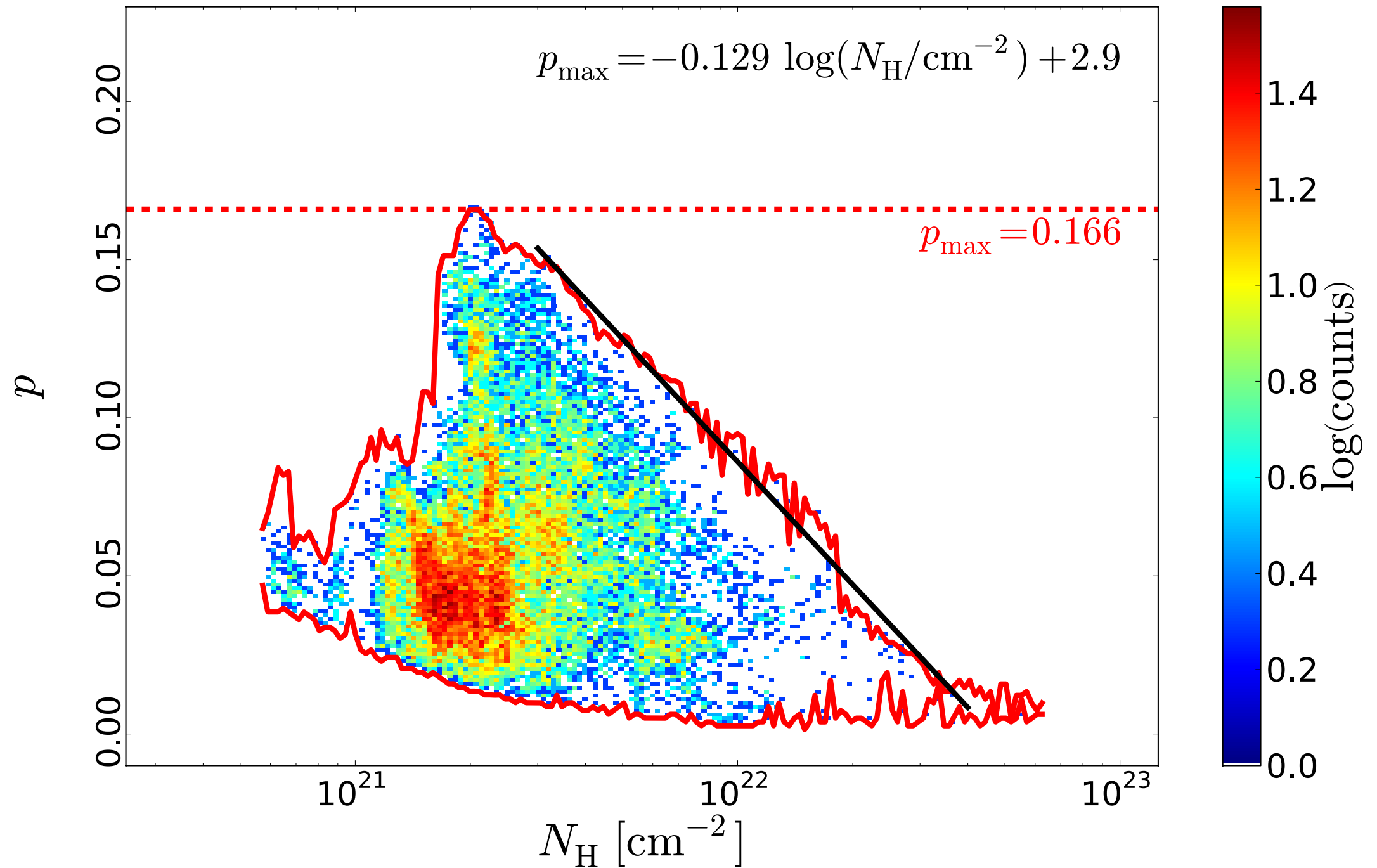
- **Simple, controlled statistics, allowing thorough parameter space exploration**
- **Points to a magnetic spectral index near 2.6 in the Polaris Flare**
- **Consistent with an approach using dust polarization C_ℓ and a model with a finite number of layers (Boulanger, Bracco, Vansyngel))**

Additional slides

Polarization fractions vs. column density

$$p/\sigma_p > 3$$

Ophiuchus

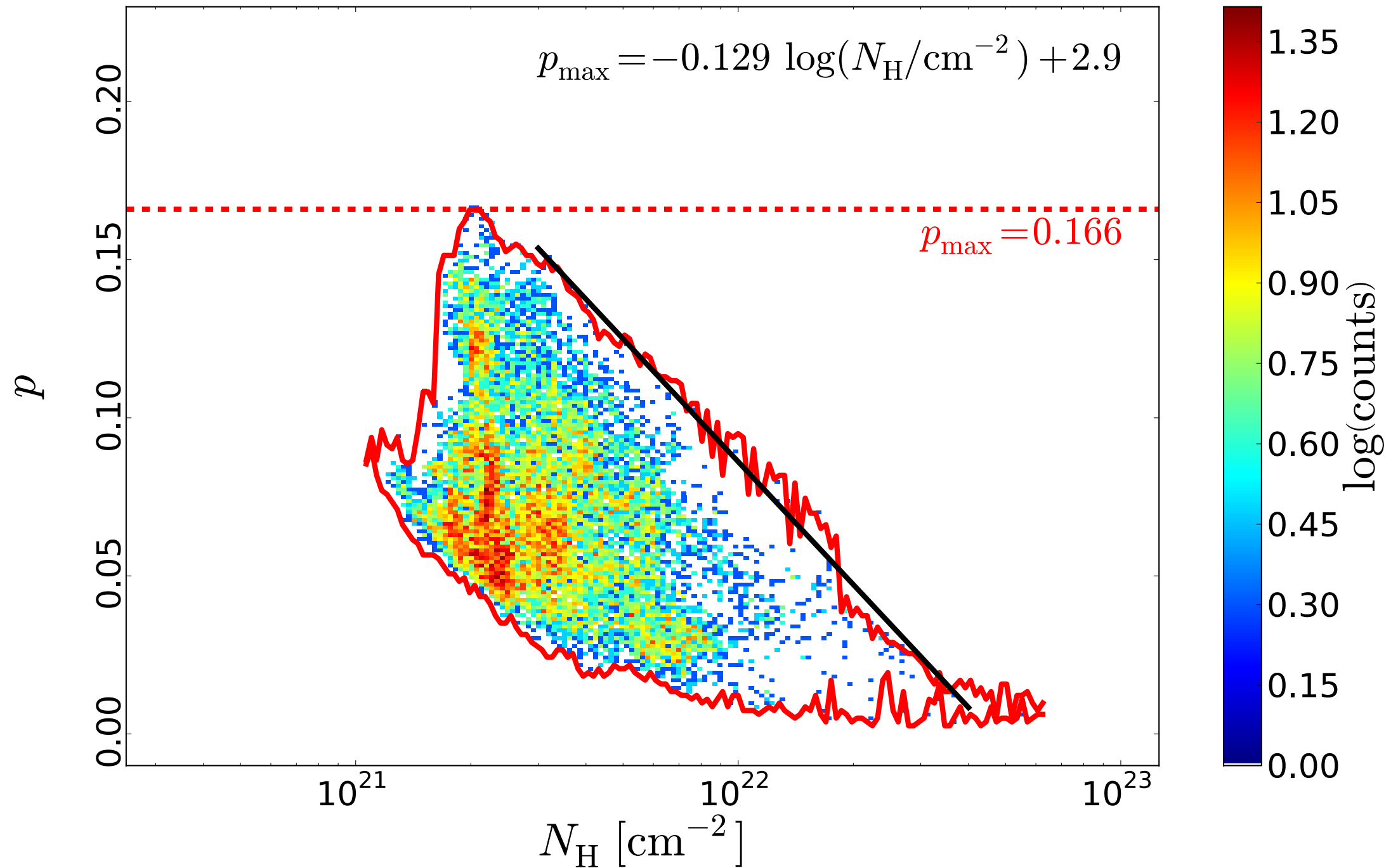


Anti-correlation robust with respect to polarization S/N

Polarization fractions vs. column density

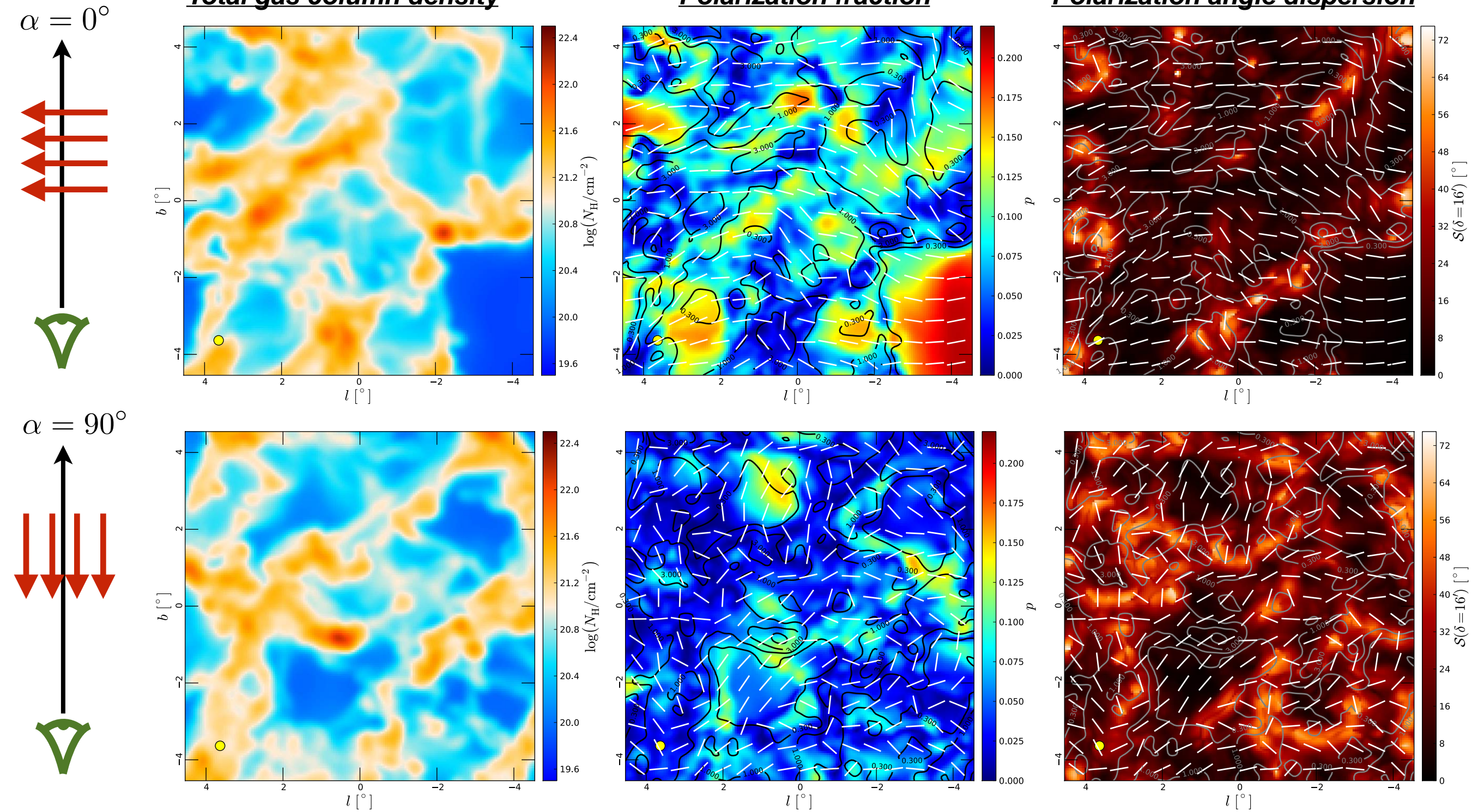
$p/\sigma_p > 10$

Ophiuchus



Anti-correlation robust with respect to polarization S/N

Simulated polarized thermal dust emission maps

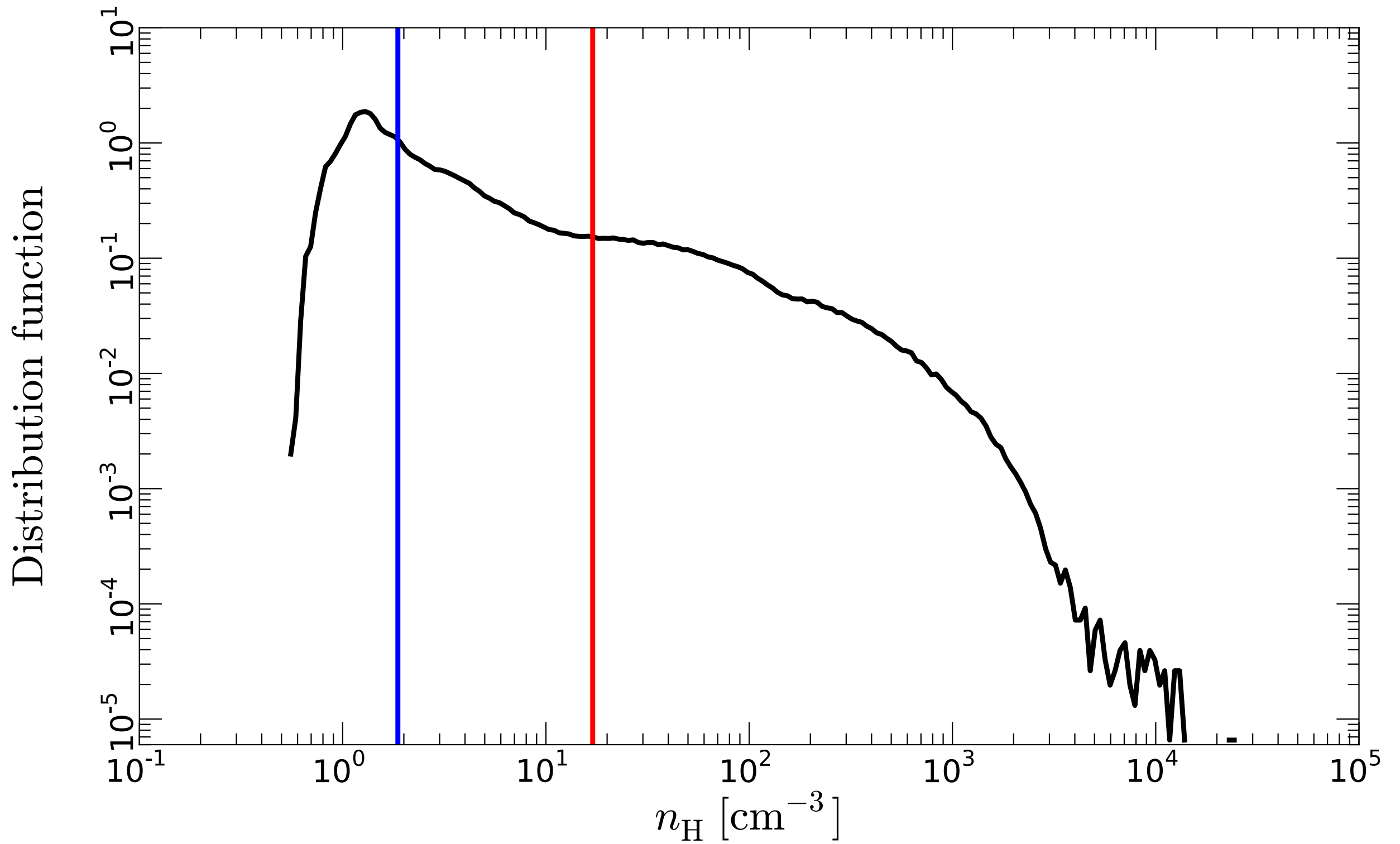


Anti-correlation p and N_{H}

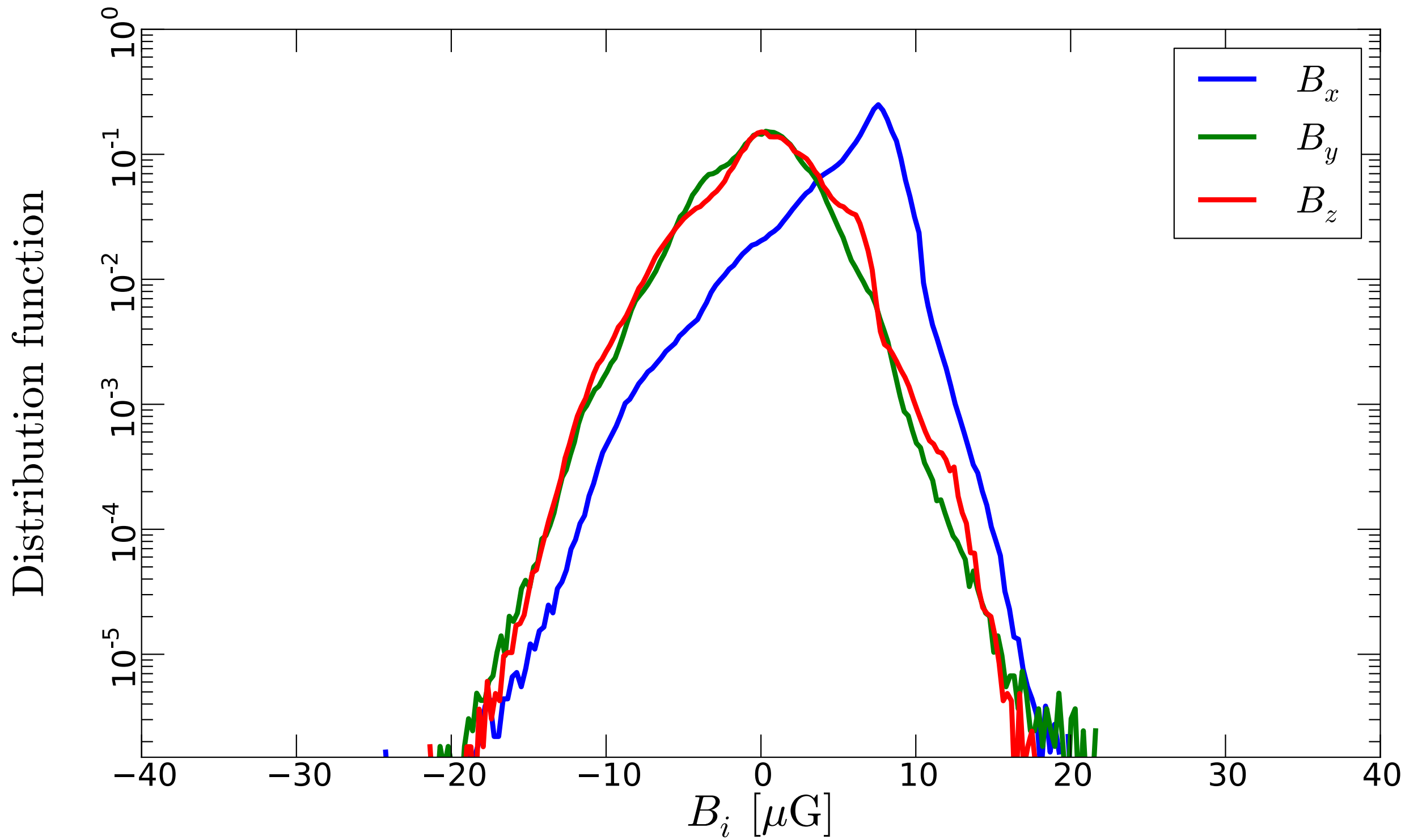
Anti-correlation p and S

Lower polarization fractions when along the mean field

MHD simulation density PDF



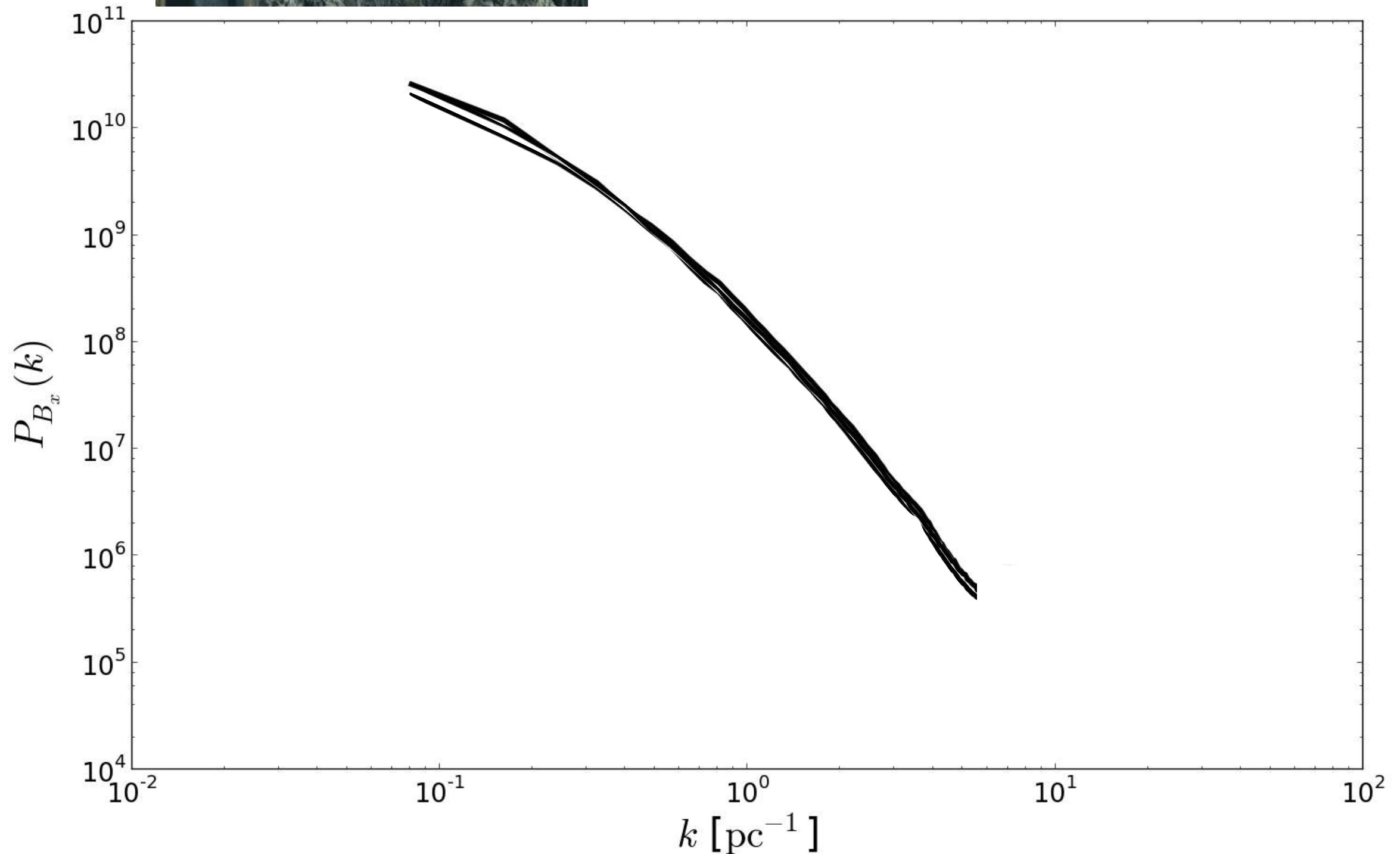
MHD simulation magnetic field PDF



MHD simulation magnetic field power spectrum



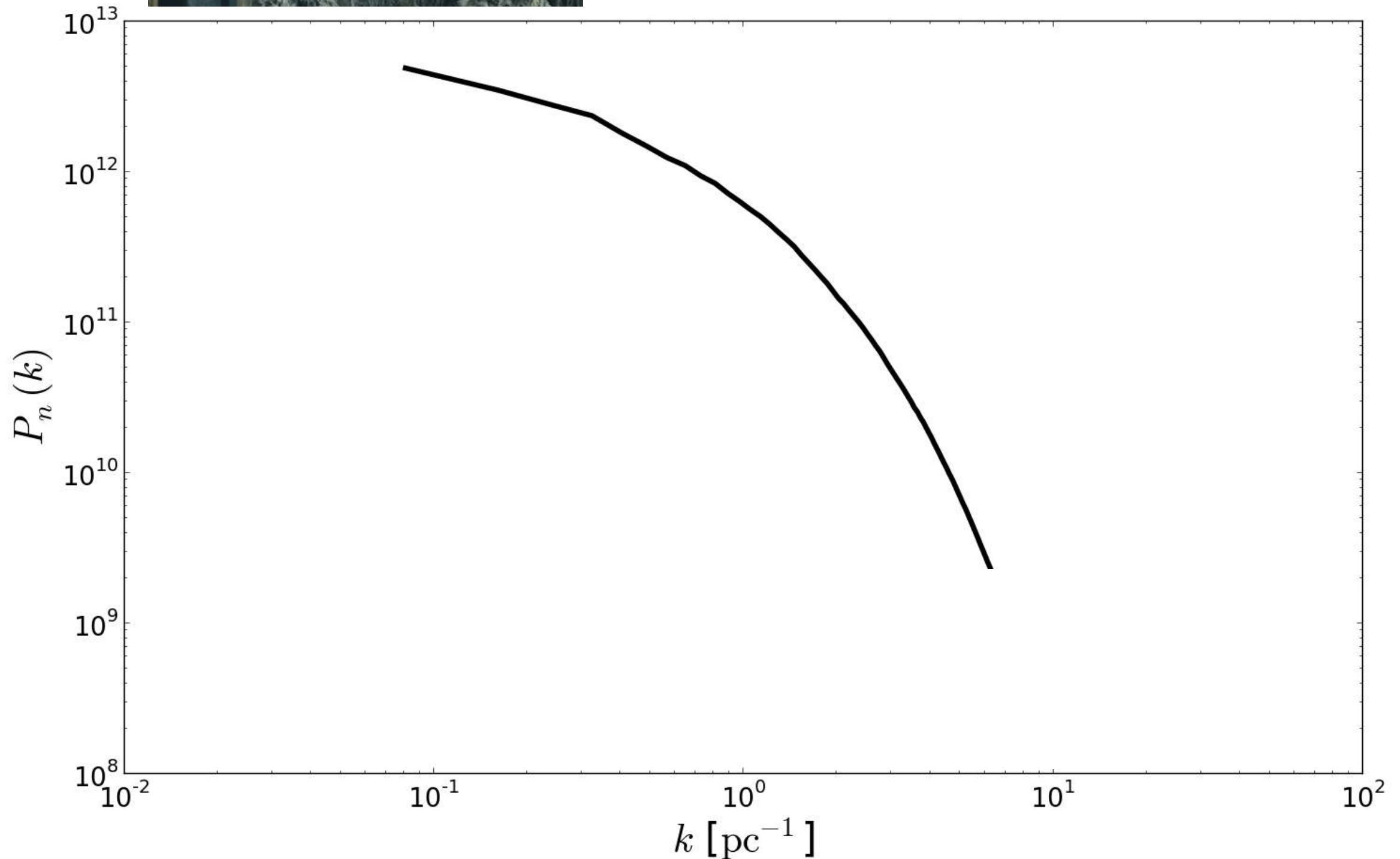
« You have no power-law here ! »



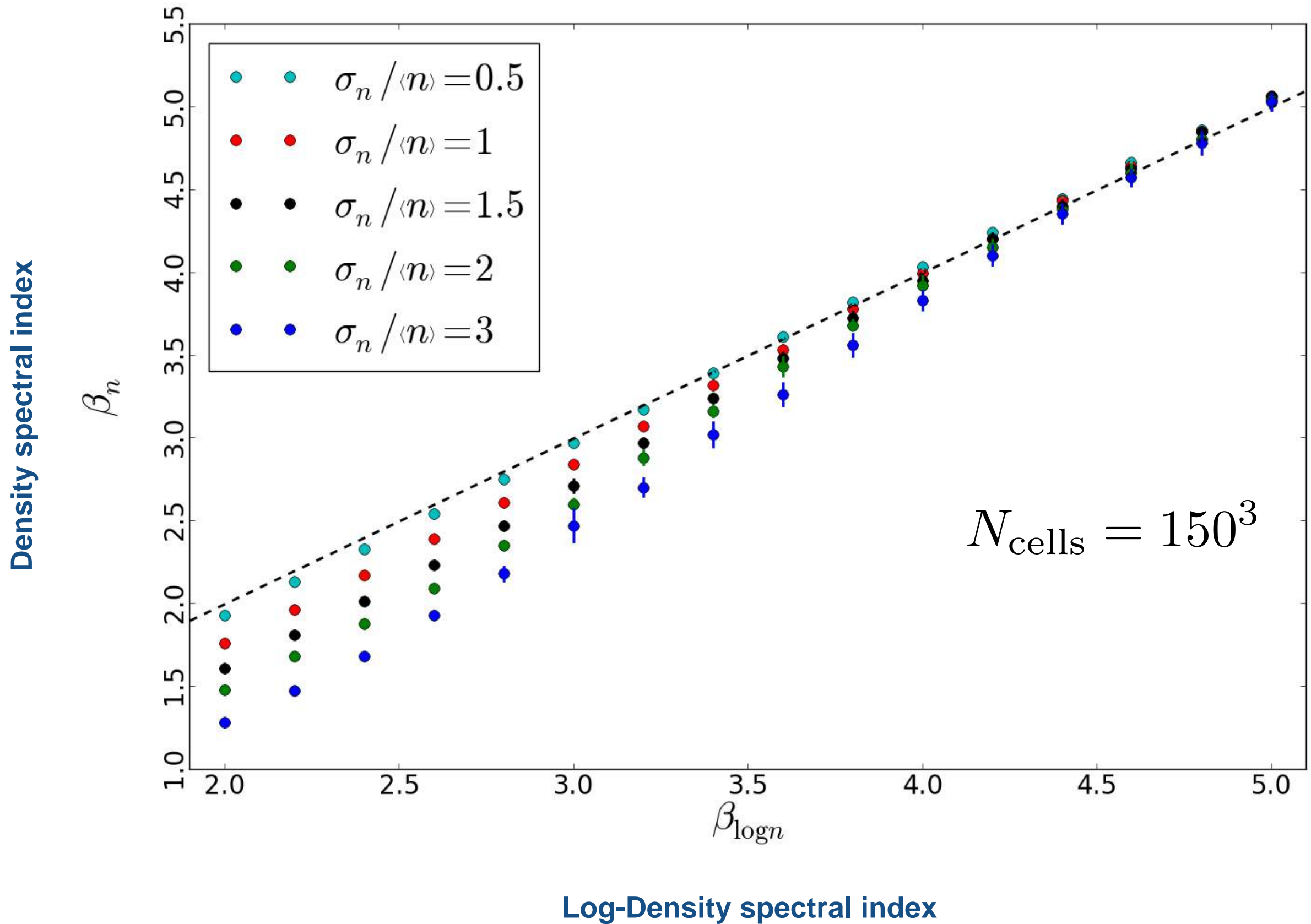
MHD simulation density power spectrum



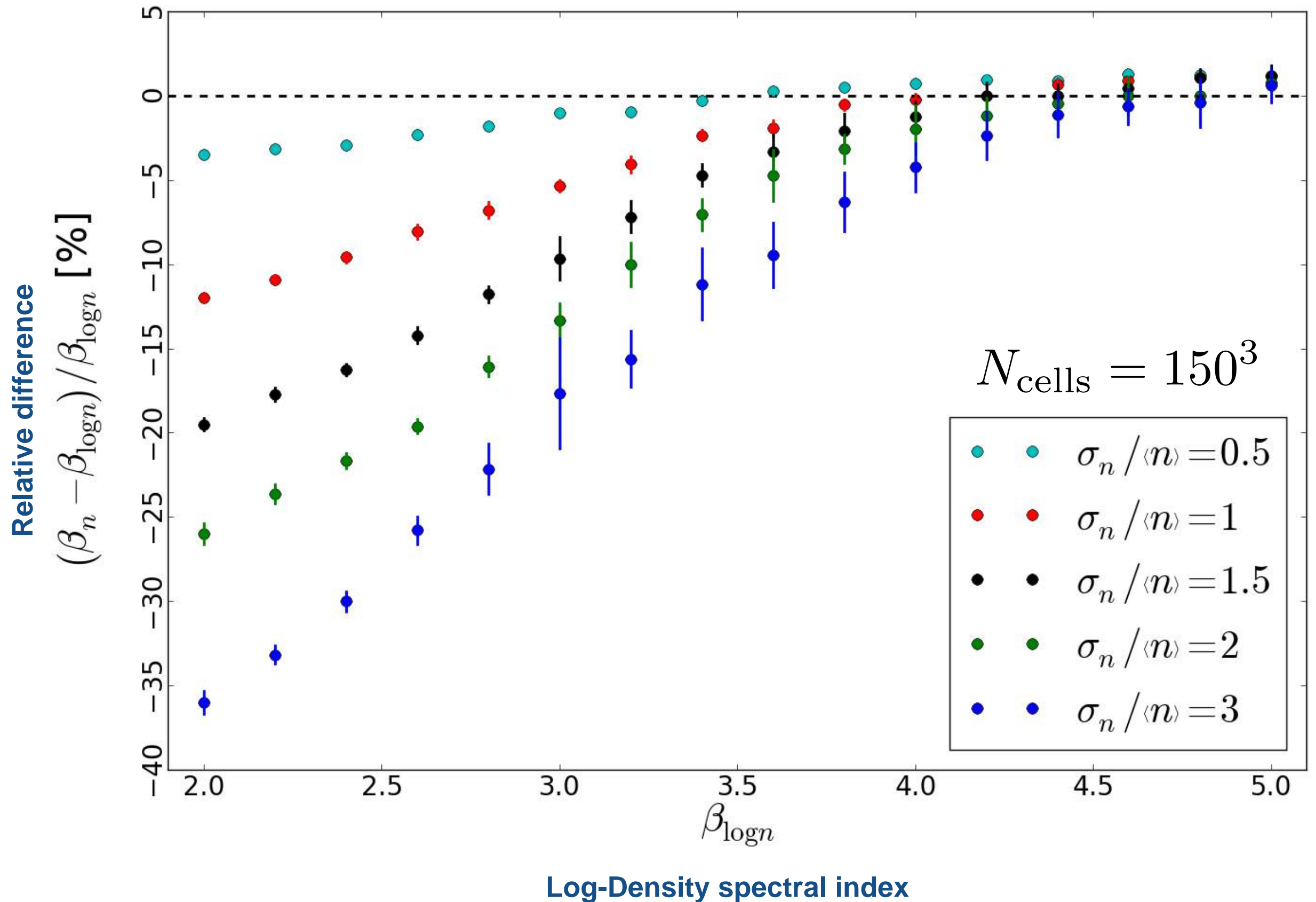
« You have no power-law here ! »



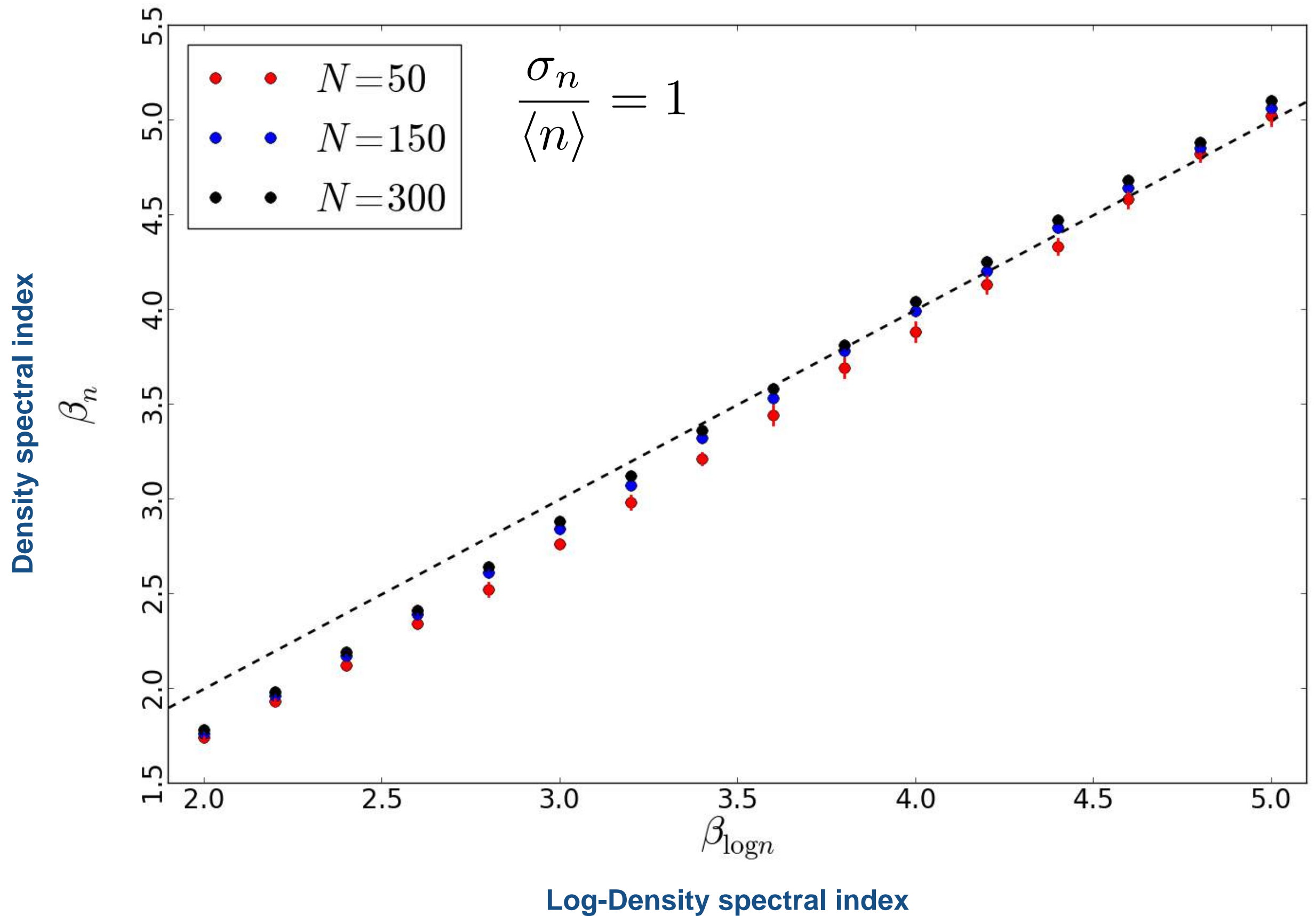
Properties of the dust density field



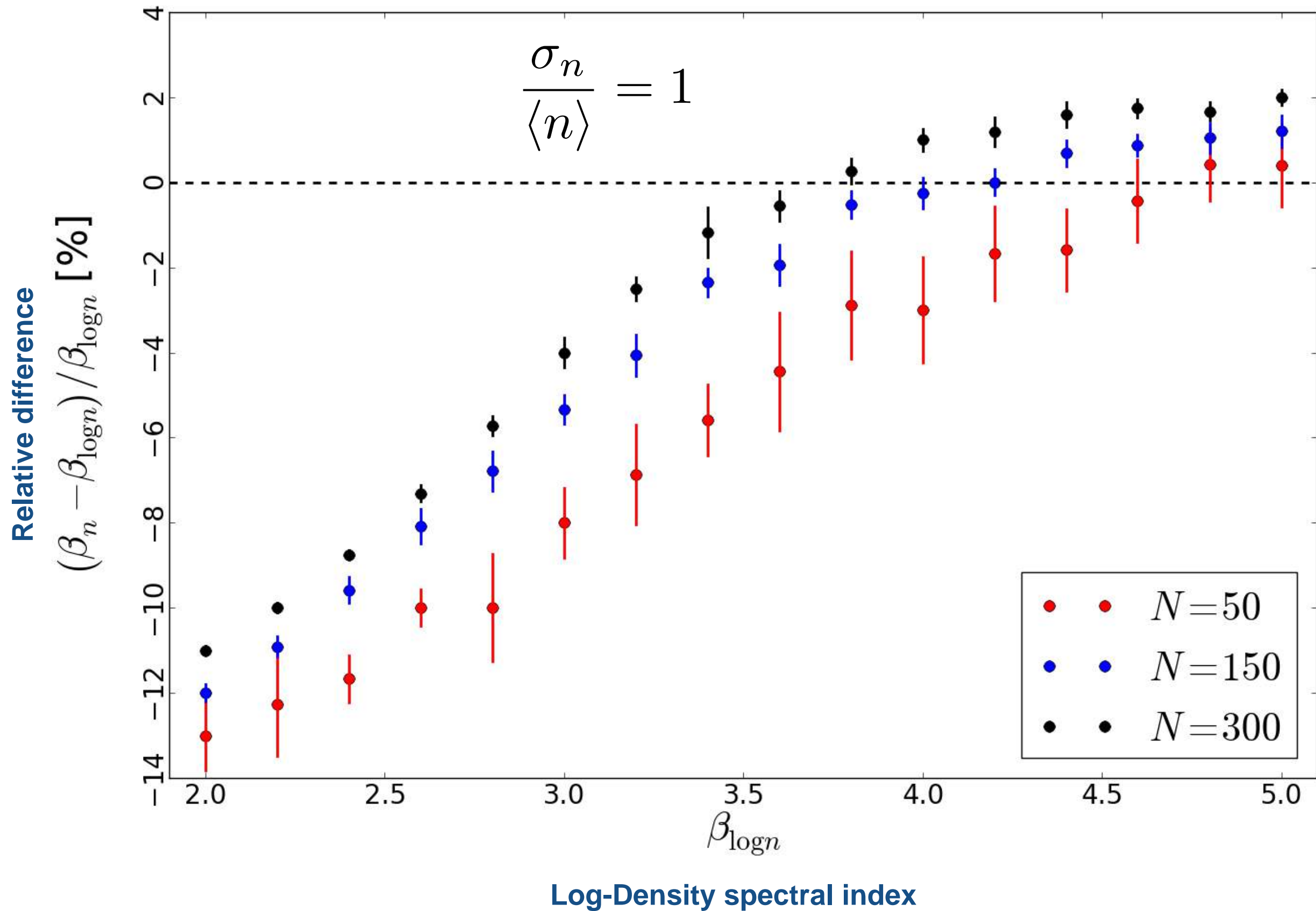
Synthetic density field properties



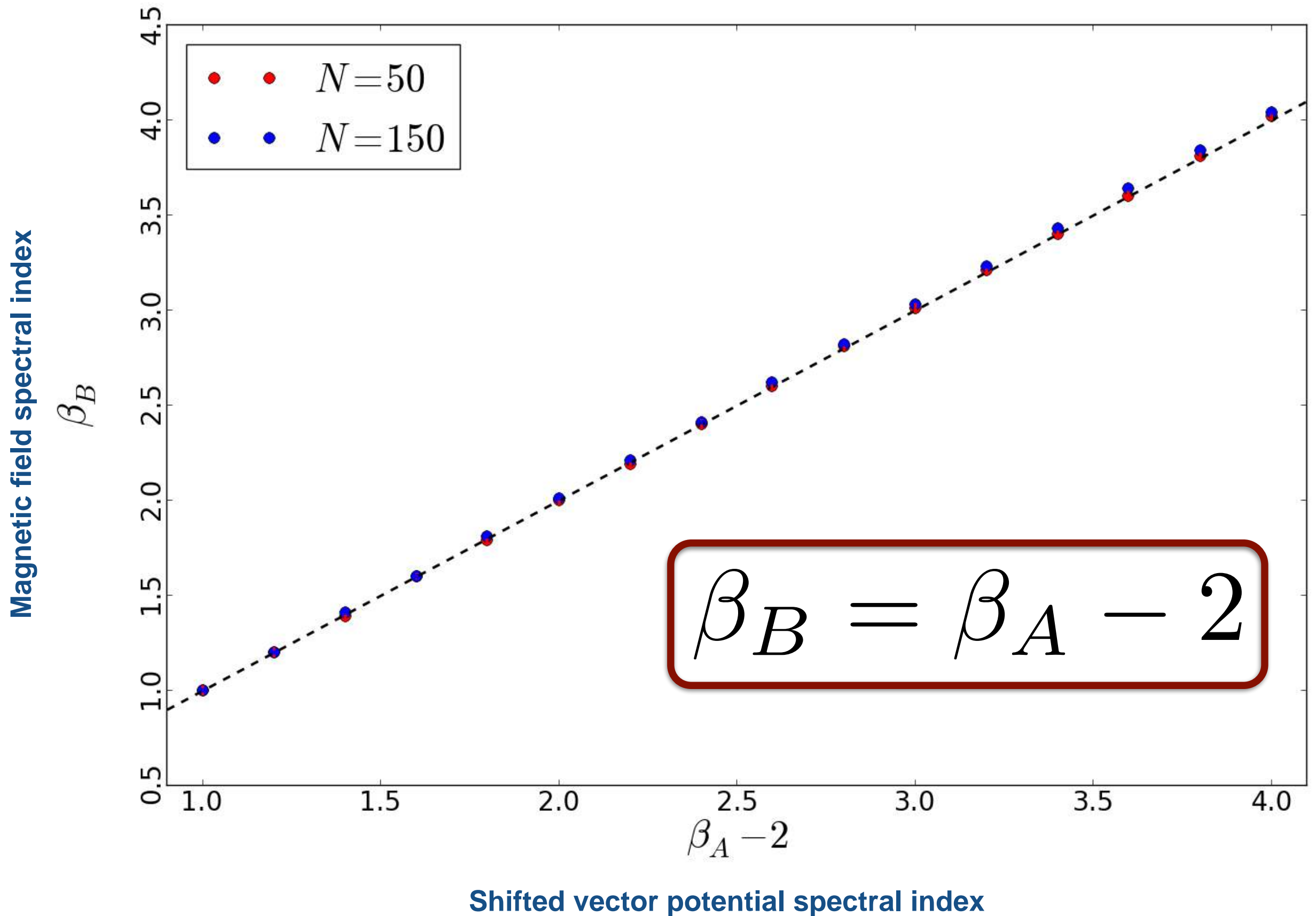
Synthetic density field properties



Synthetic density field properties

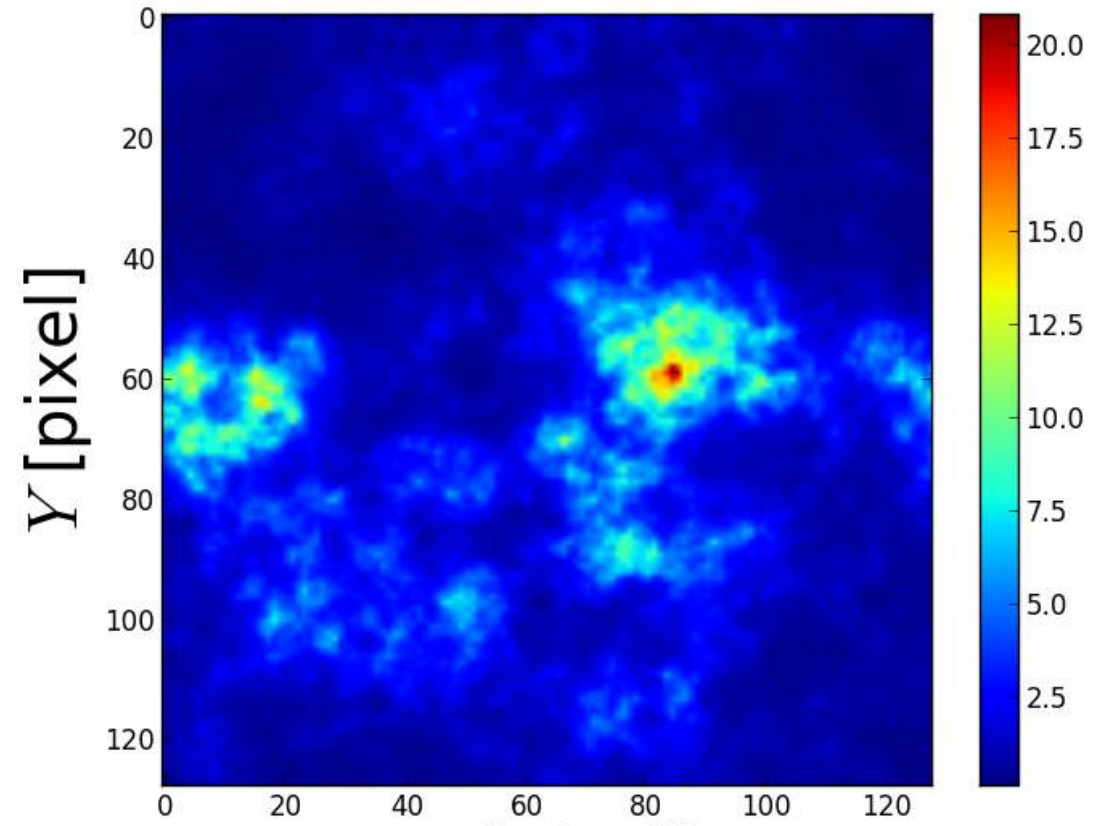
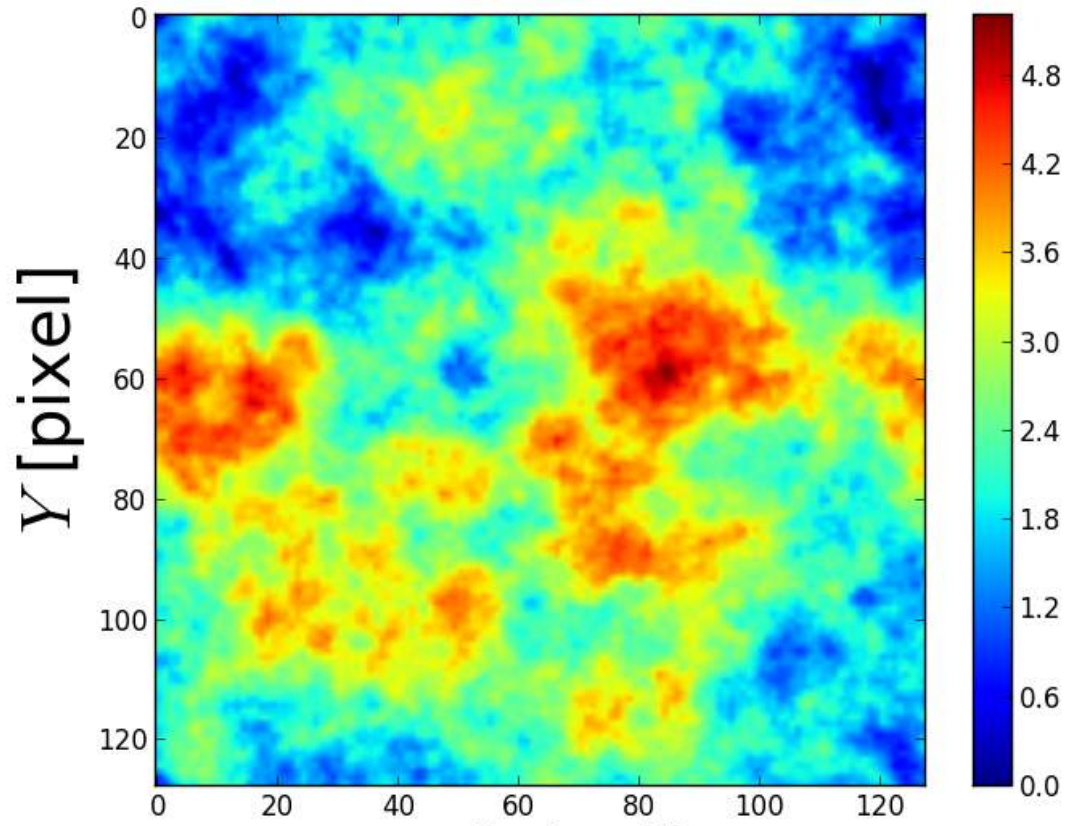


Synthetic magnetic field spectral index

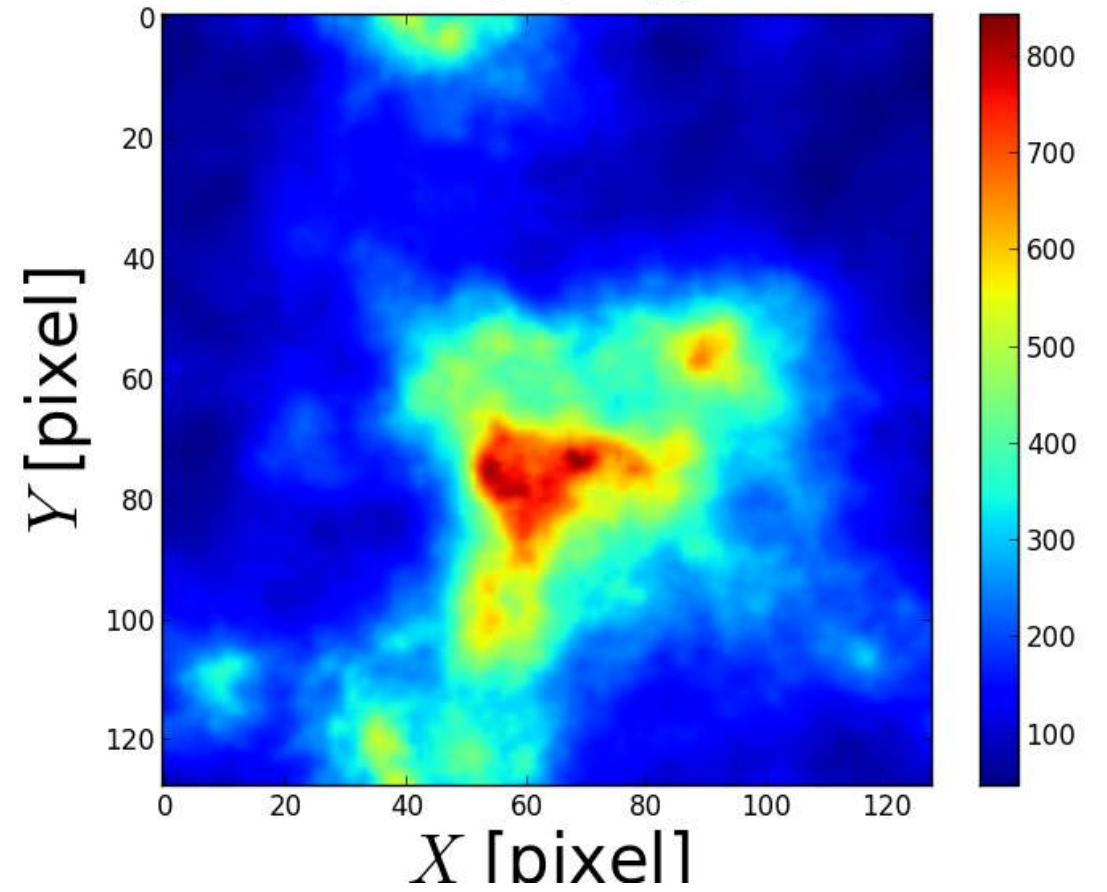
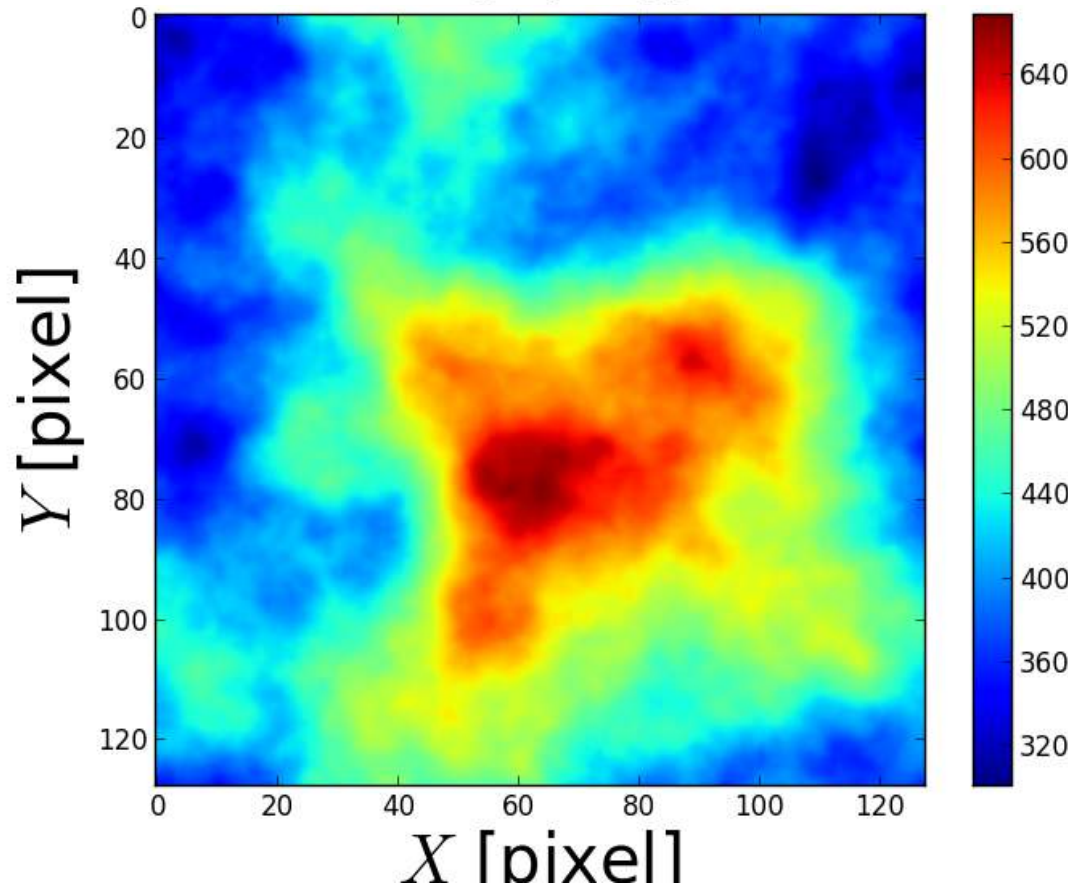


fBm and exponentiated fBm

Slice of a 128x128x128 cube



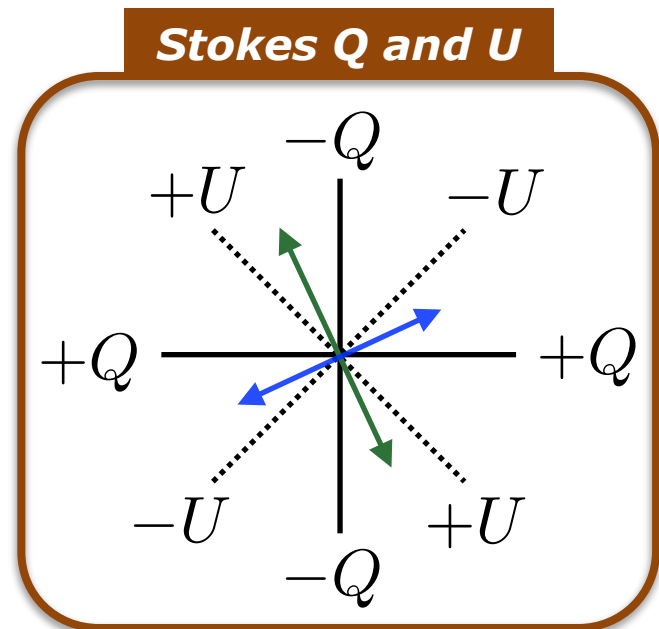
Integration along one axis



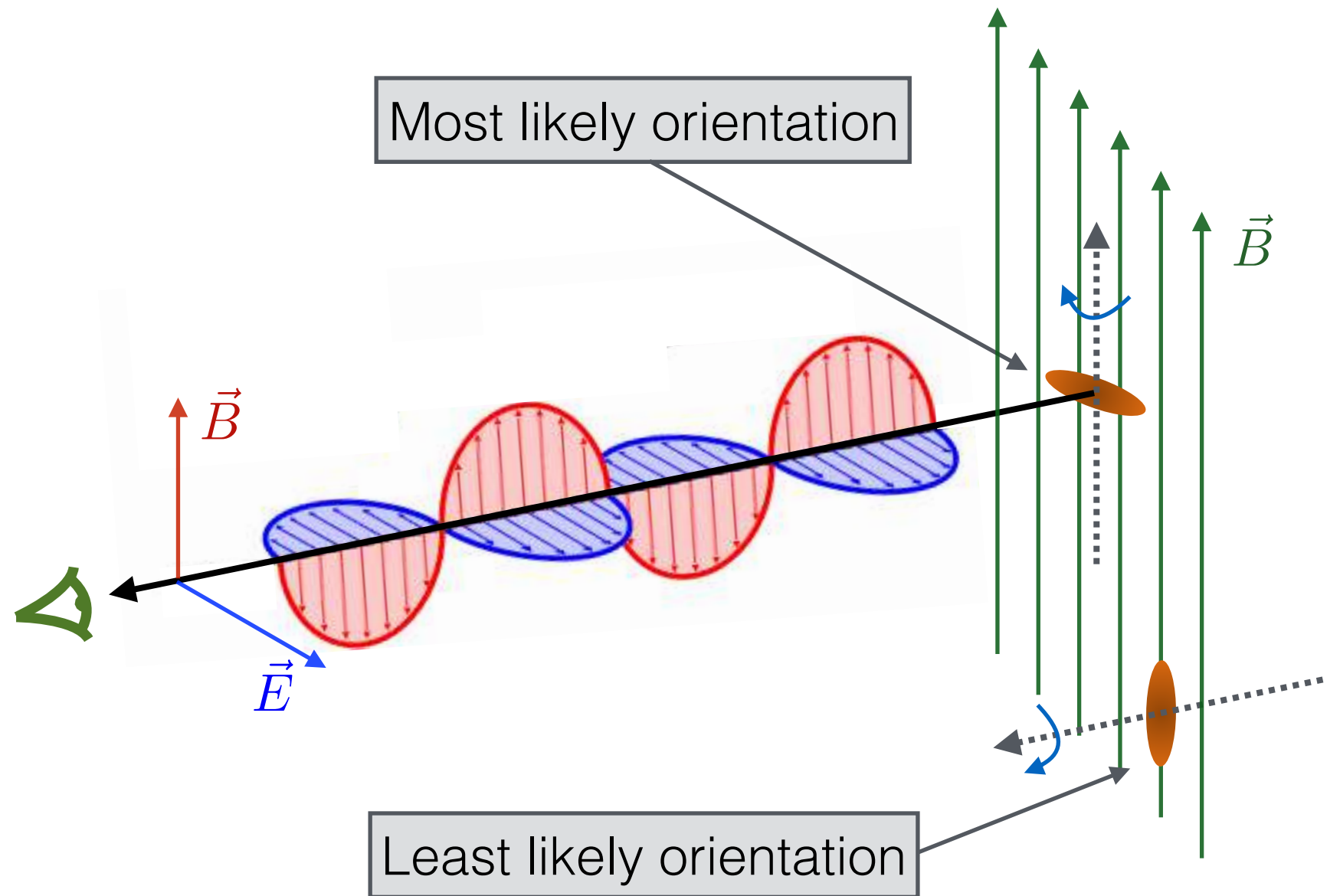
fBm

exponentiated fBm

Polarized thermal dust emission essentials



Polarization orientation
Magnetic field orientation



- Grains are aspherical, charged, rotating, and aligned preferentially perpendicularly to the local magnetic field
- Cross sections are proportional to the size, so grains emit more radiation parallel to their long axes
- Polarized thermal emission arises, with an orientation perpendicular to the local magnetic field

See Thiem Hoang's and François Boulanger's talks